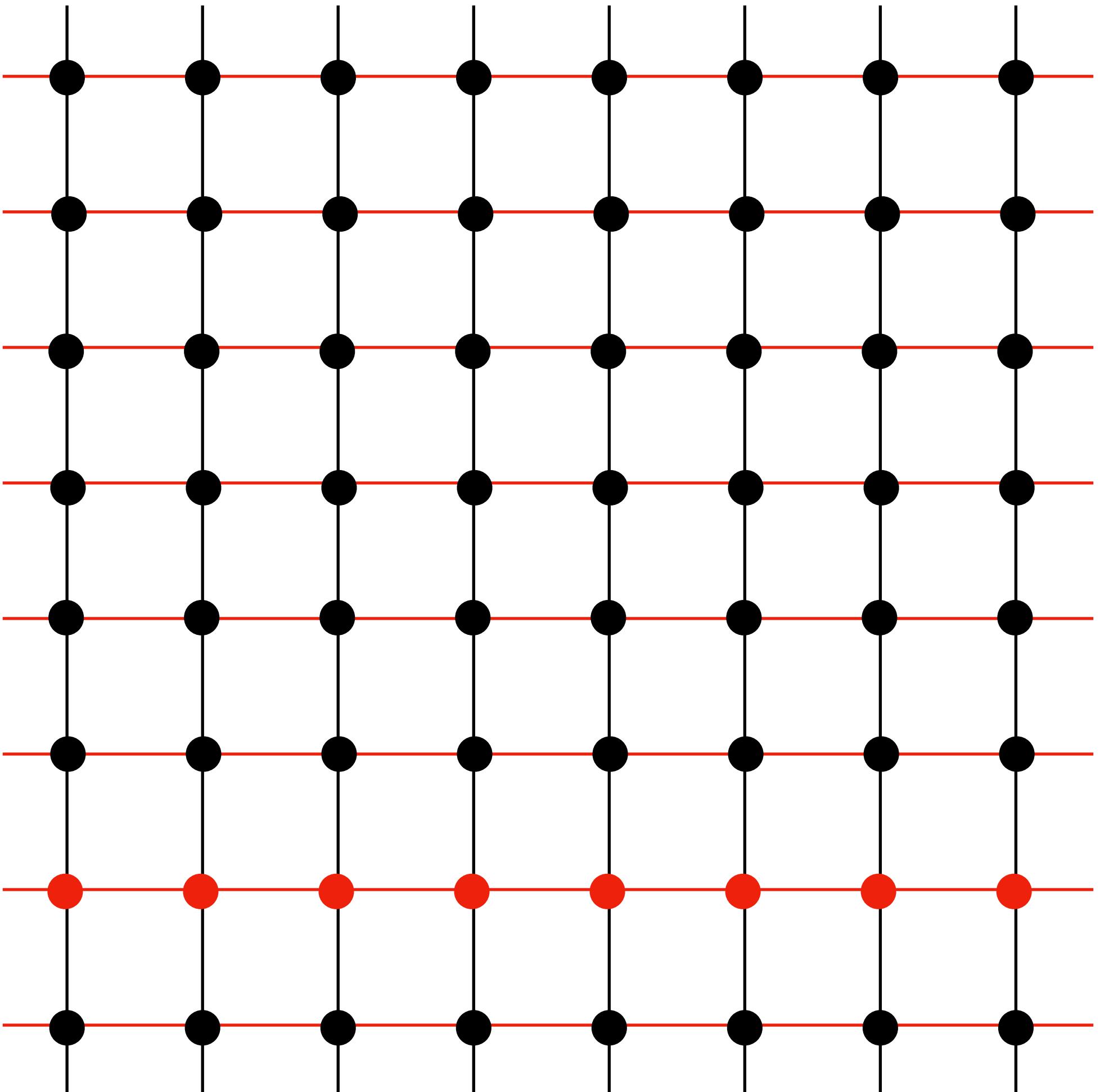
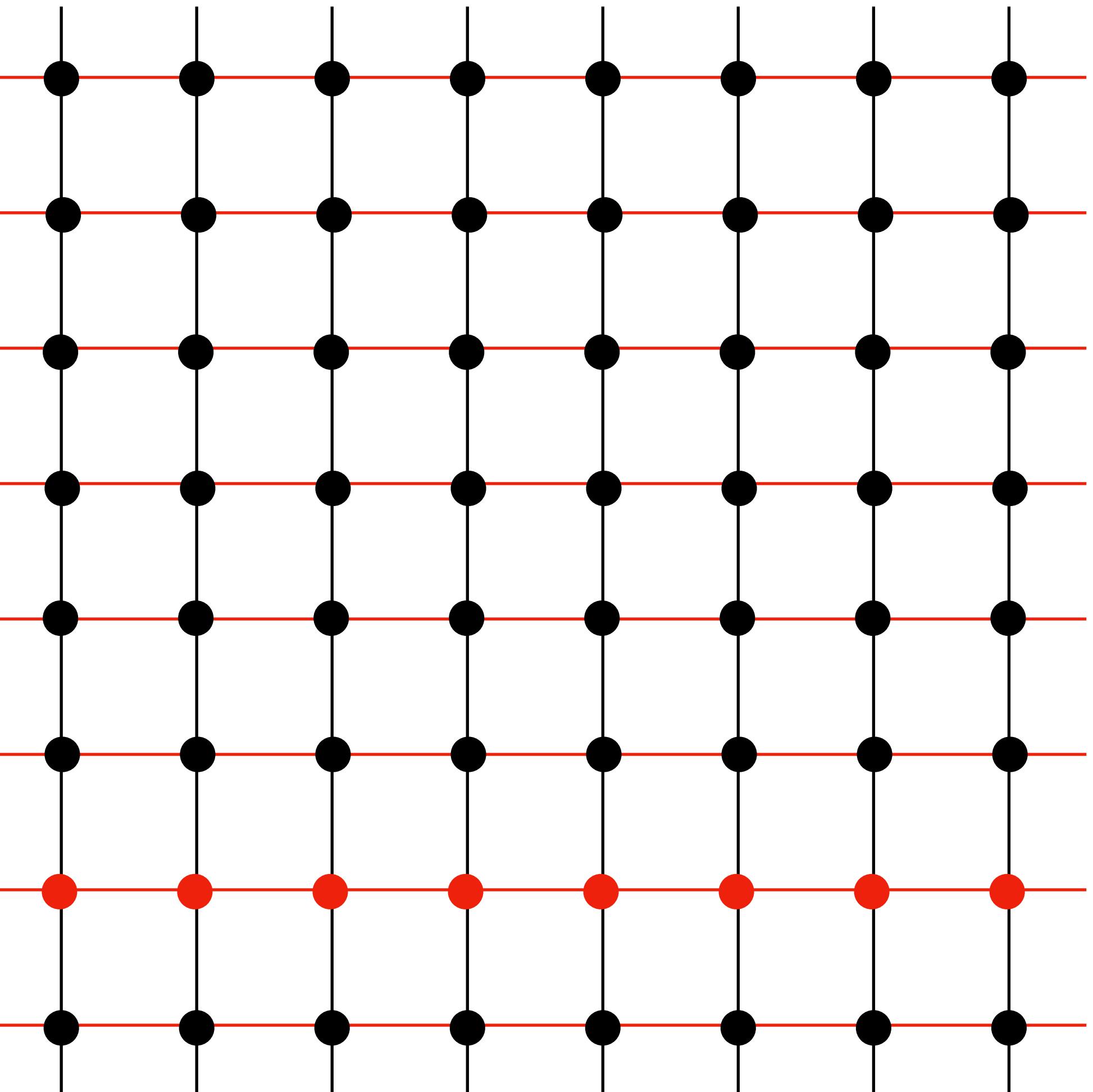


All computed in parallel



← All computed in parallel  
(in series with previous row)

Height limited by cycles

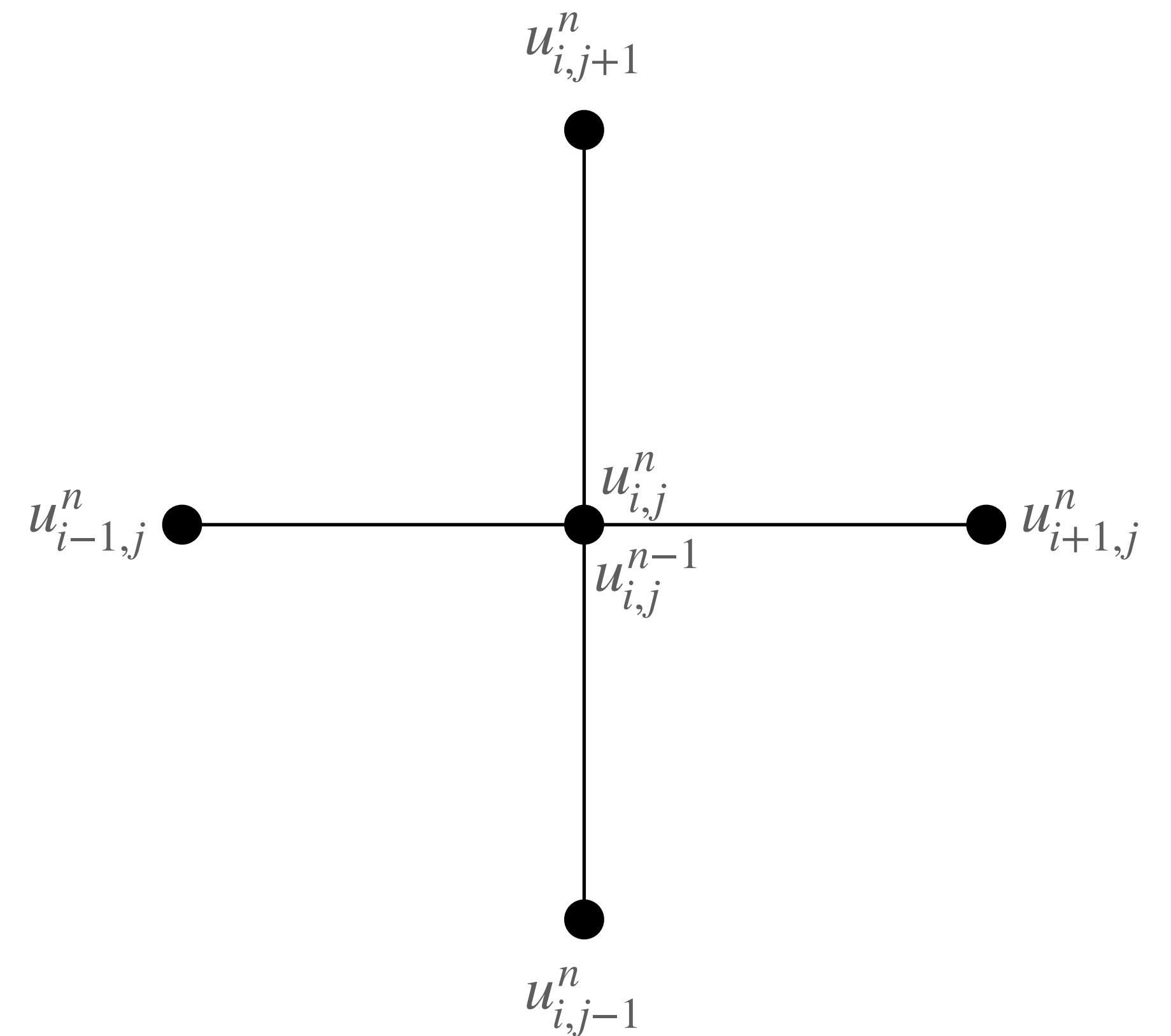


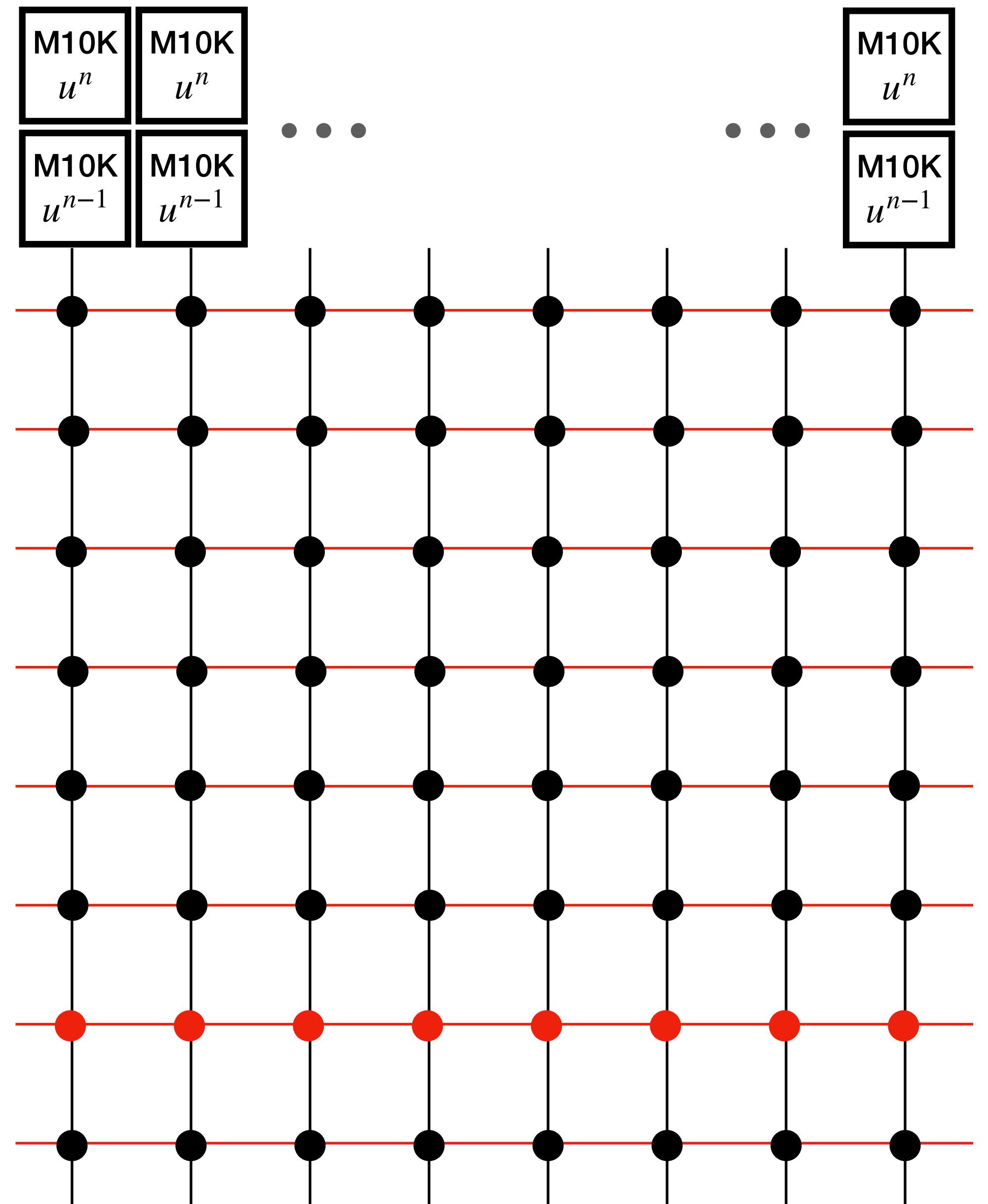
Width limited by hardware

### Compute Module

Inputs:  $u_{i,j}^n, u_{i,j}^{n-1}, u_{i-1,j}, u_{i+1,j}, u_{i,j+1}, u_{i,j-1}$   
Output:  $u_{i,j}^{n+1}$

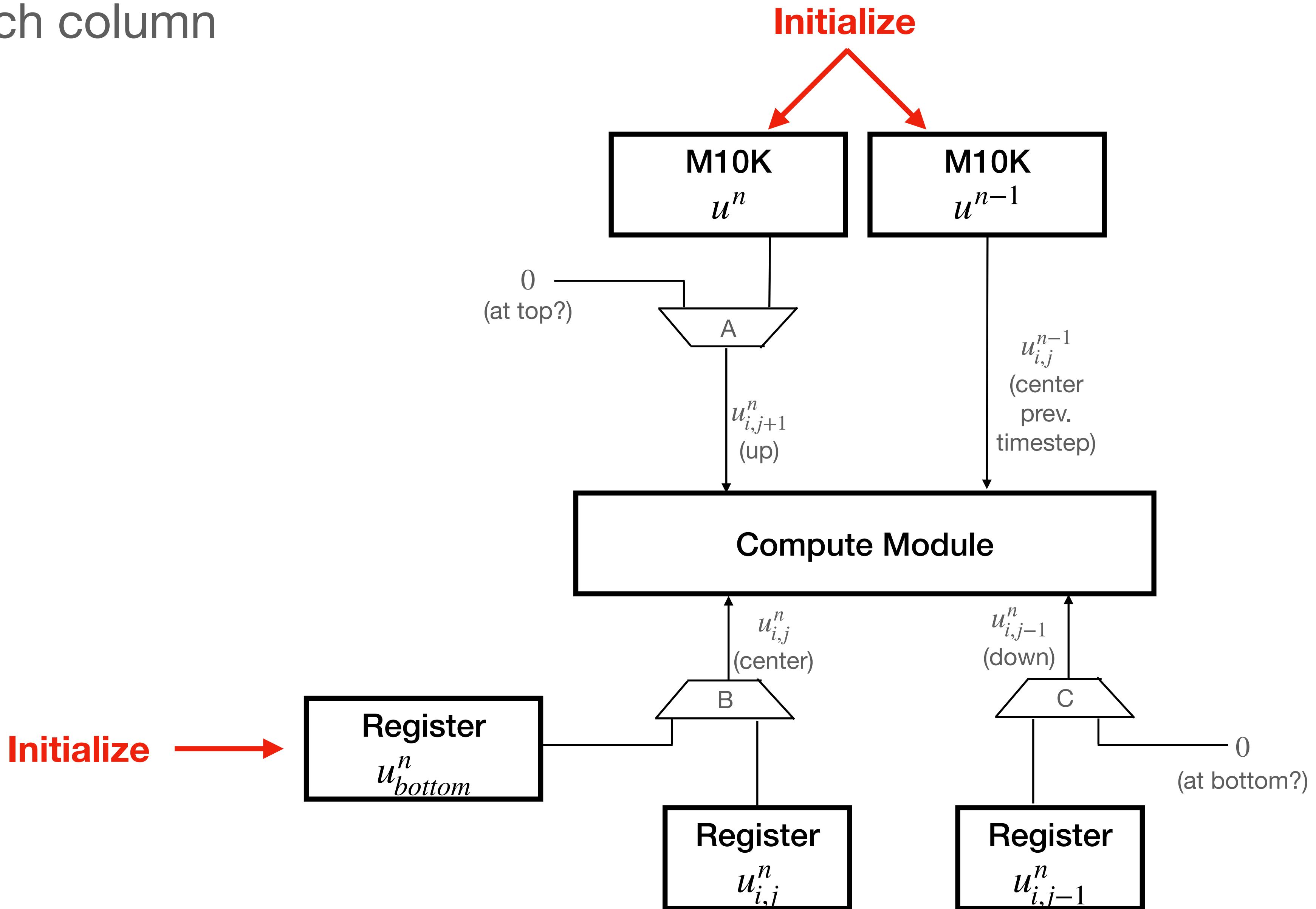
$$u_{i,j}^{n+1} = \left[1 - \frac{\eta\Delta t}{2}\right] \left\{ \rho \left[ u_{i+1,j}^n + u_{i-1,j}^n + u_{i,j-1}^n + u_{i,j+1}^n - 4u_{i,j}^n \right] + 2u_{i,j}^n - \left[1 - \frac{\eta\Delta t}{2}\right] u_{i,j}^{n-1} \right\}$$



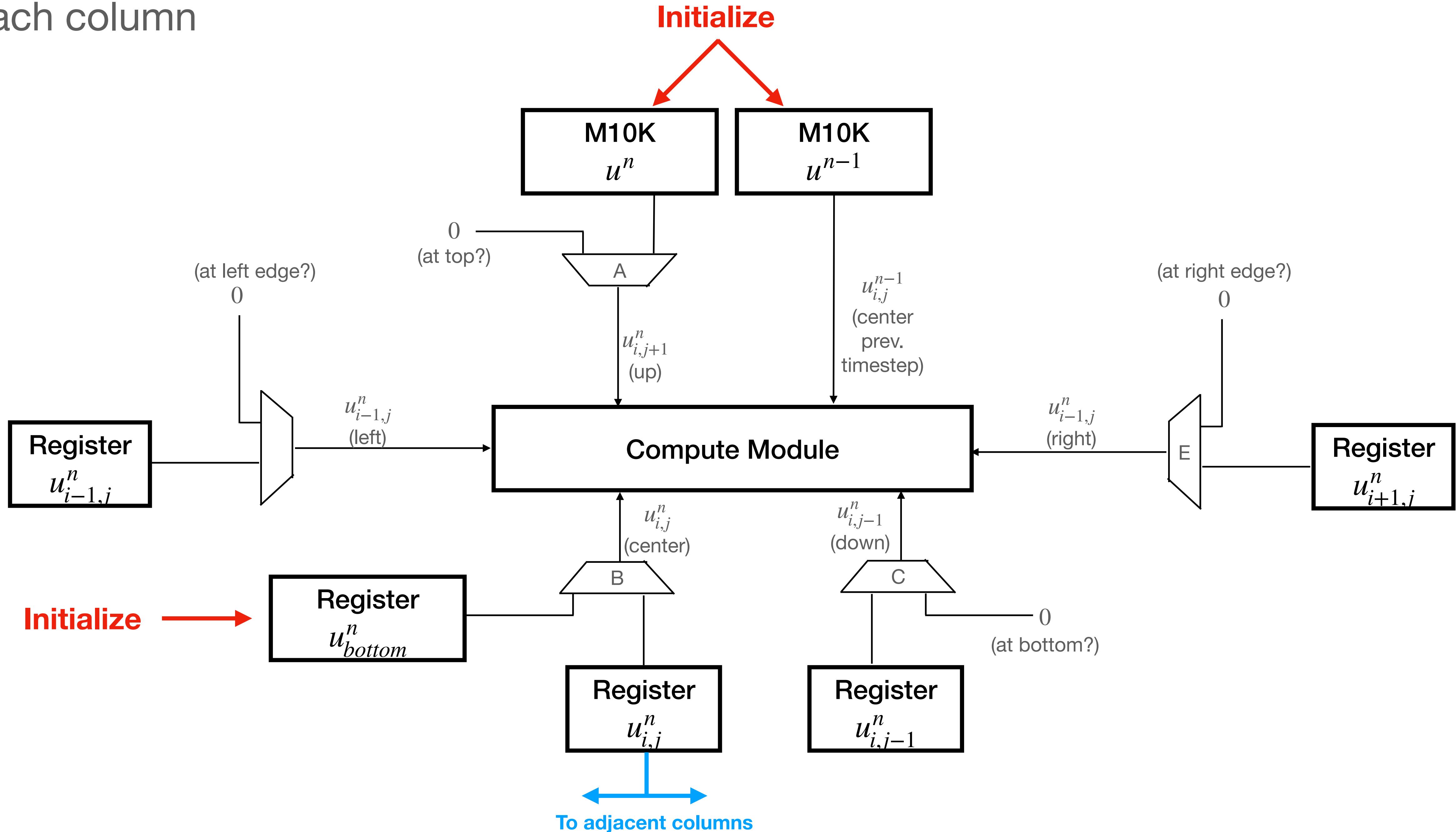


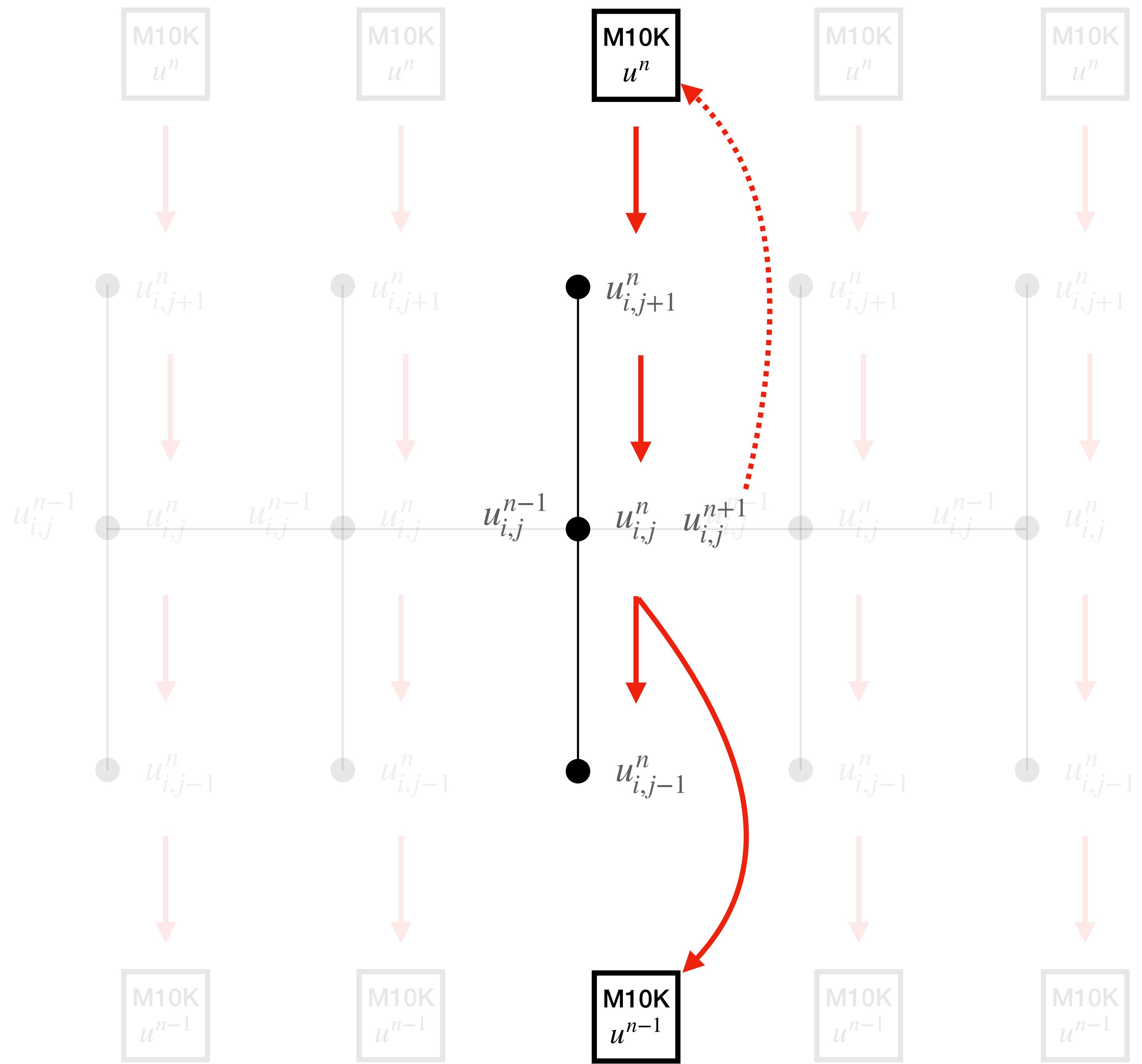
Two M10k blocks for each column

For each column

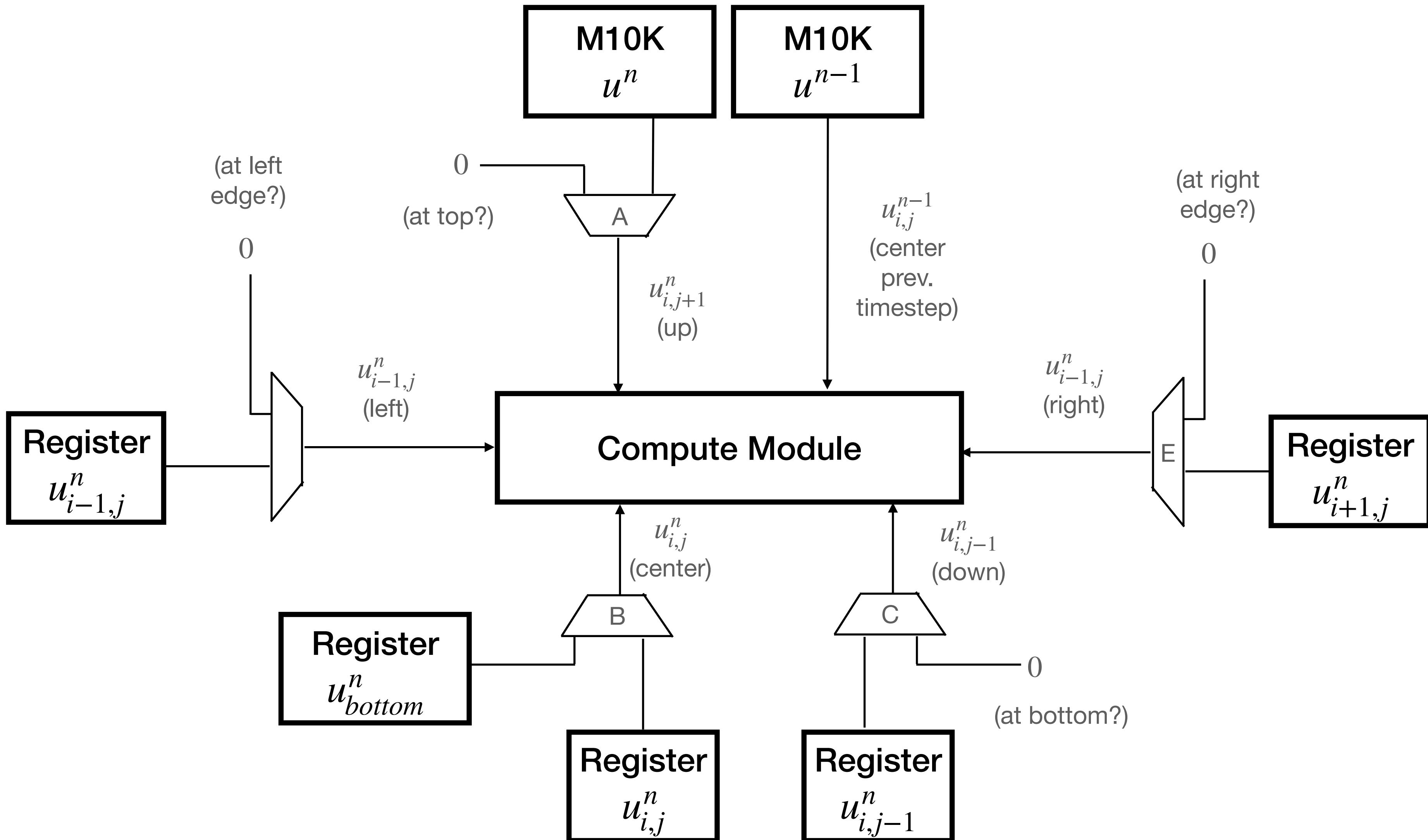
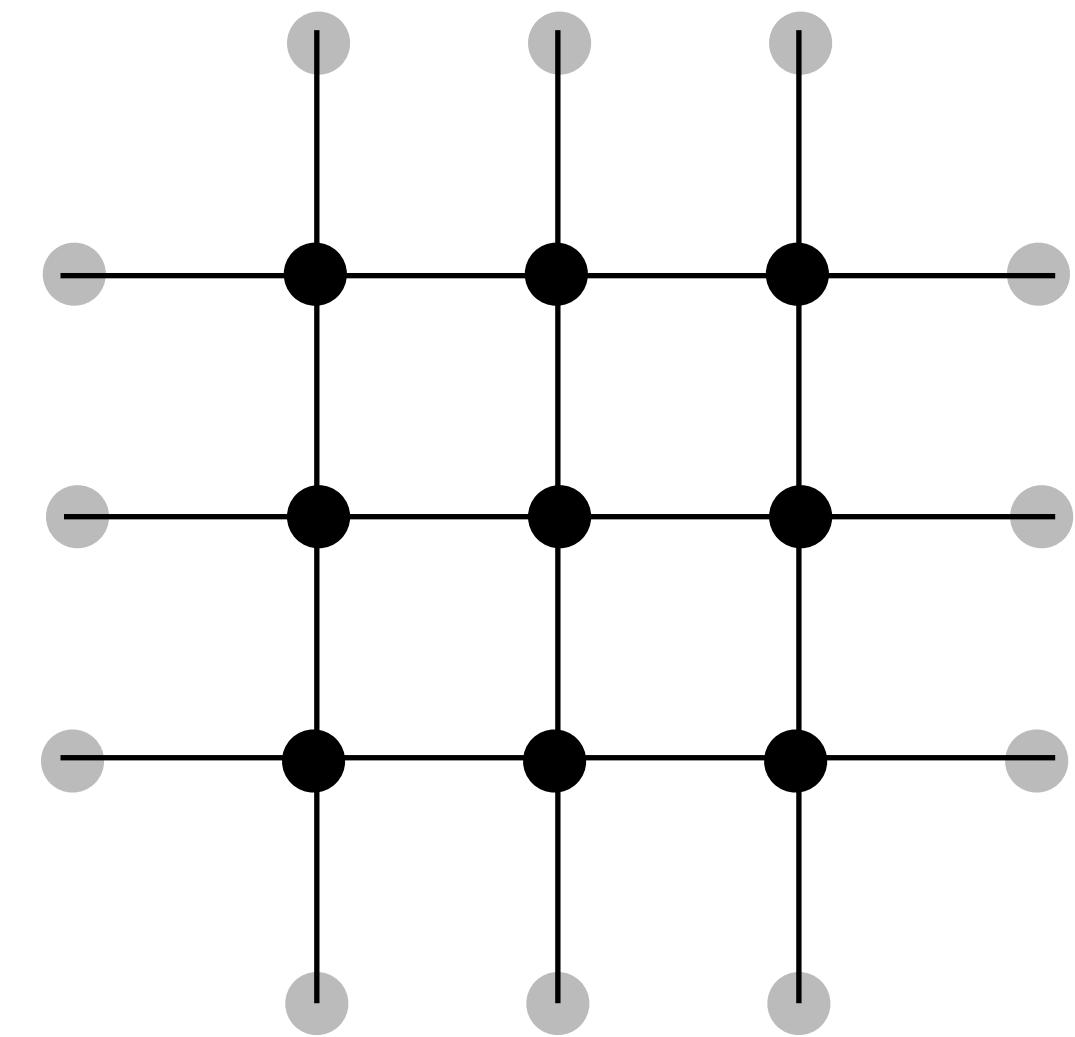


For each column

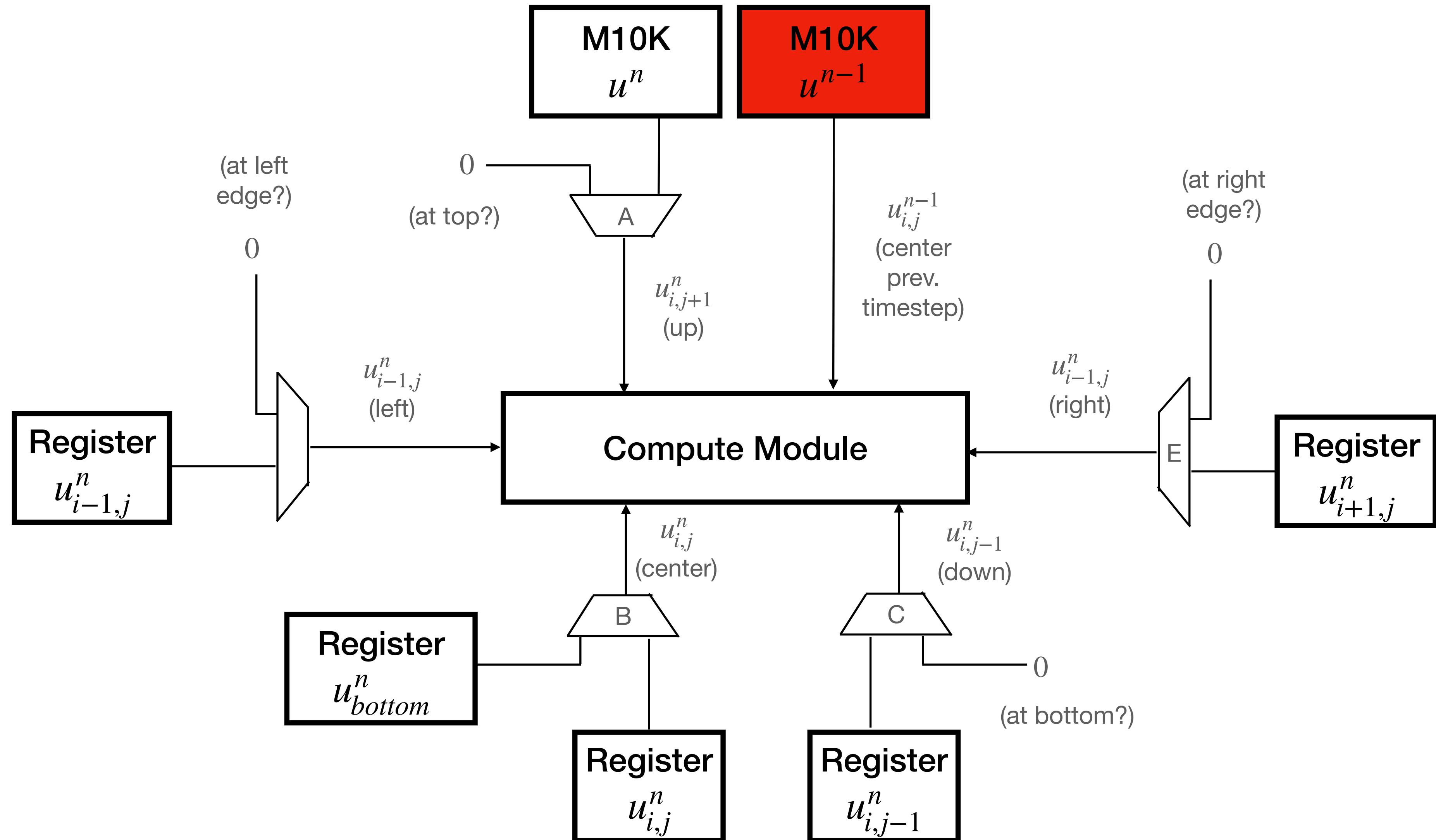
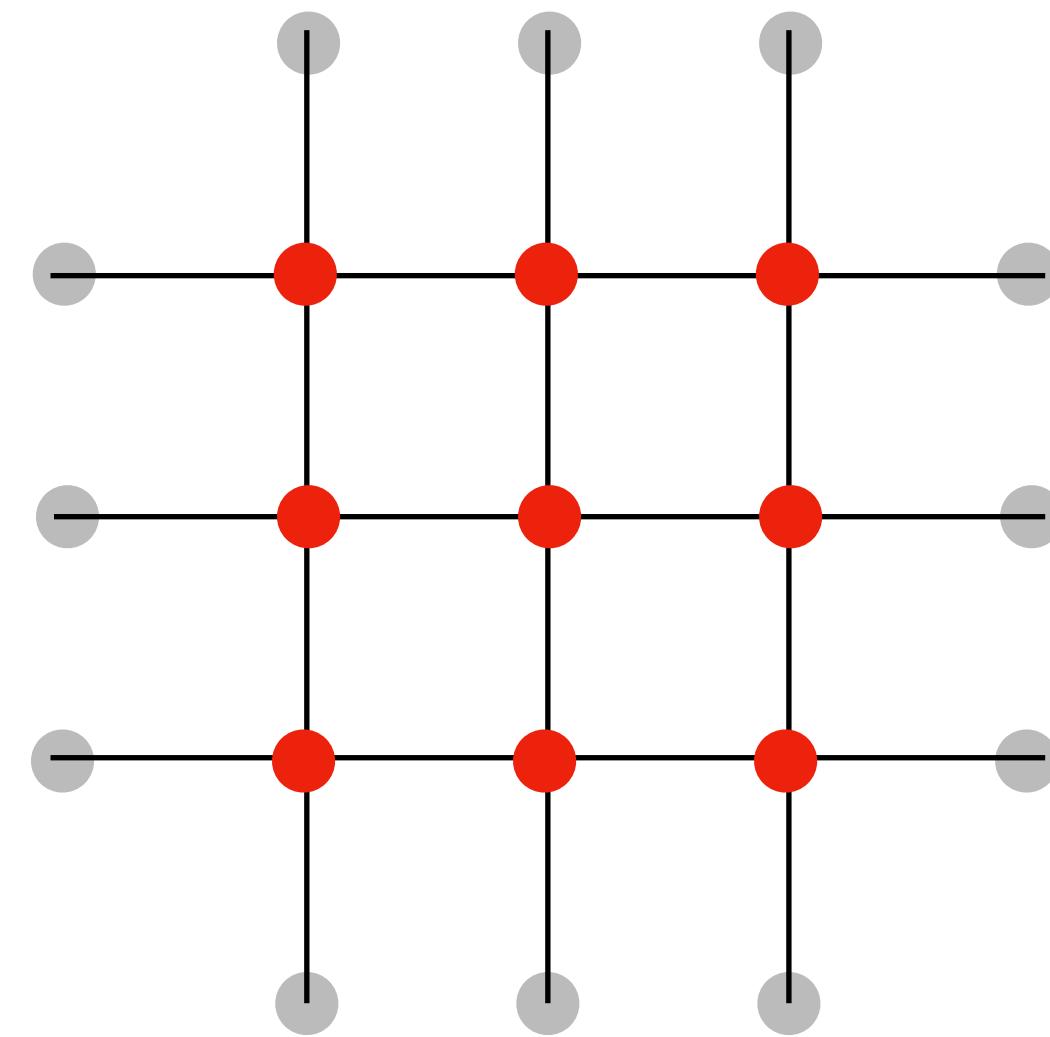




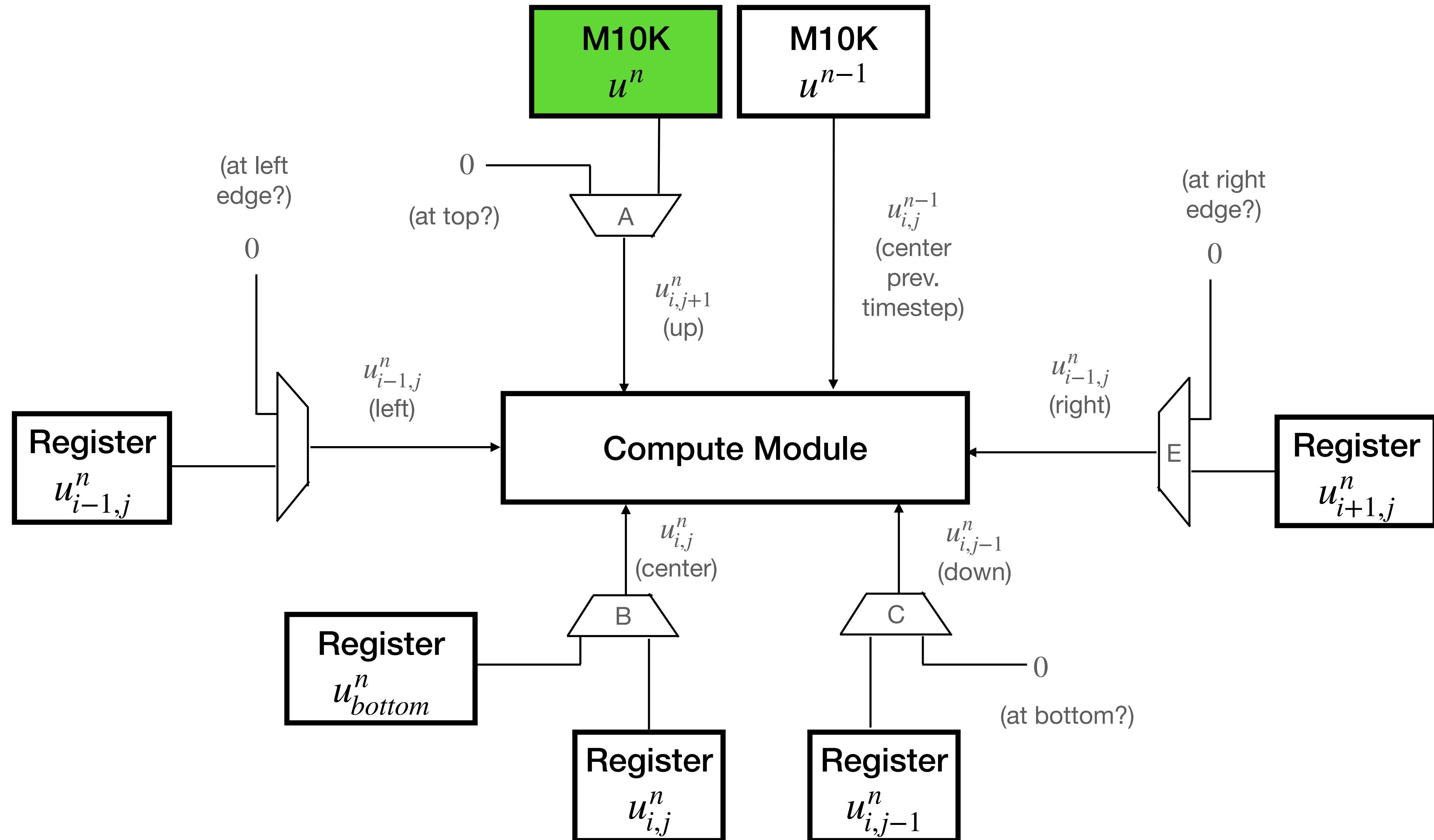
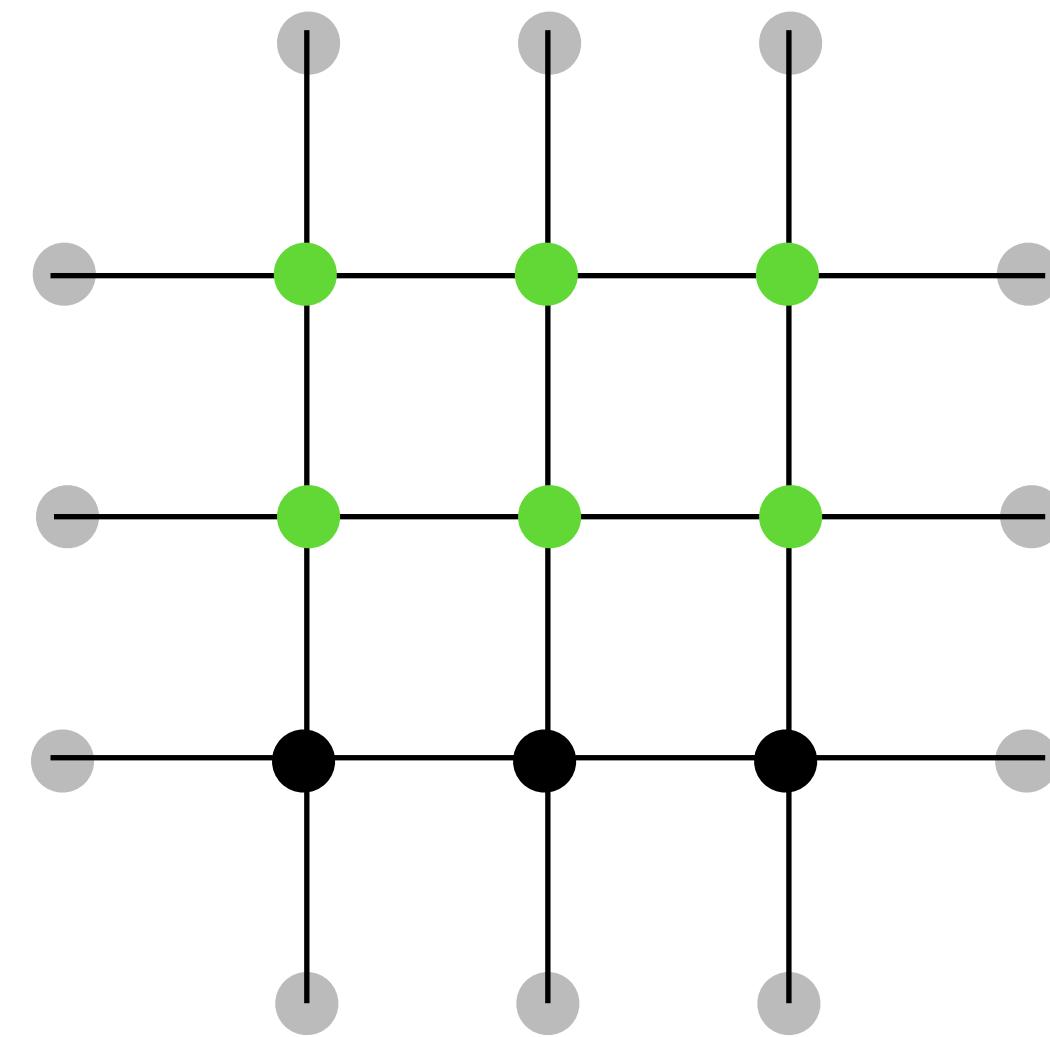
# Updating a 3x3 drum



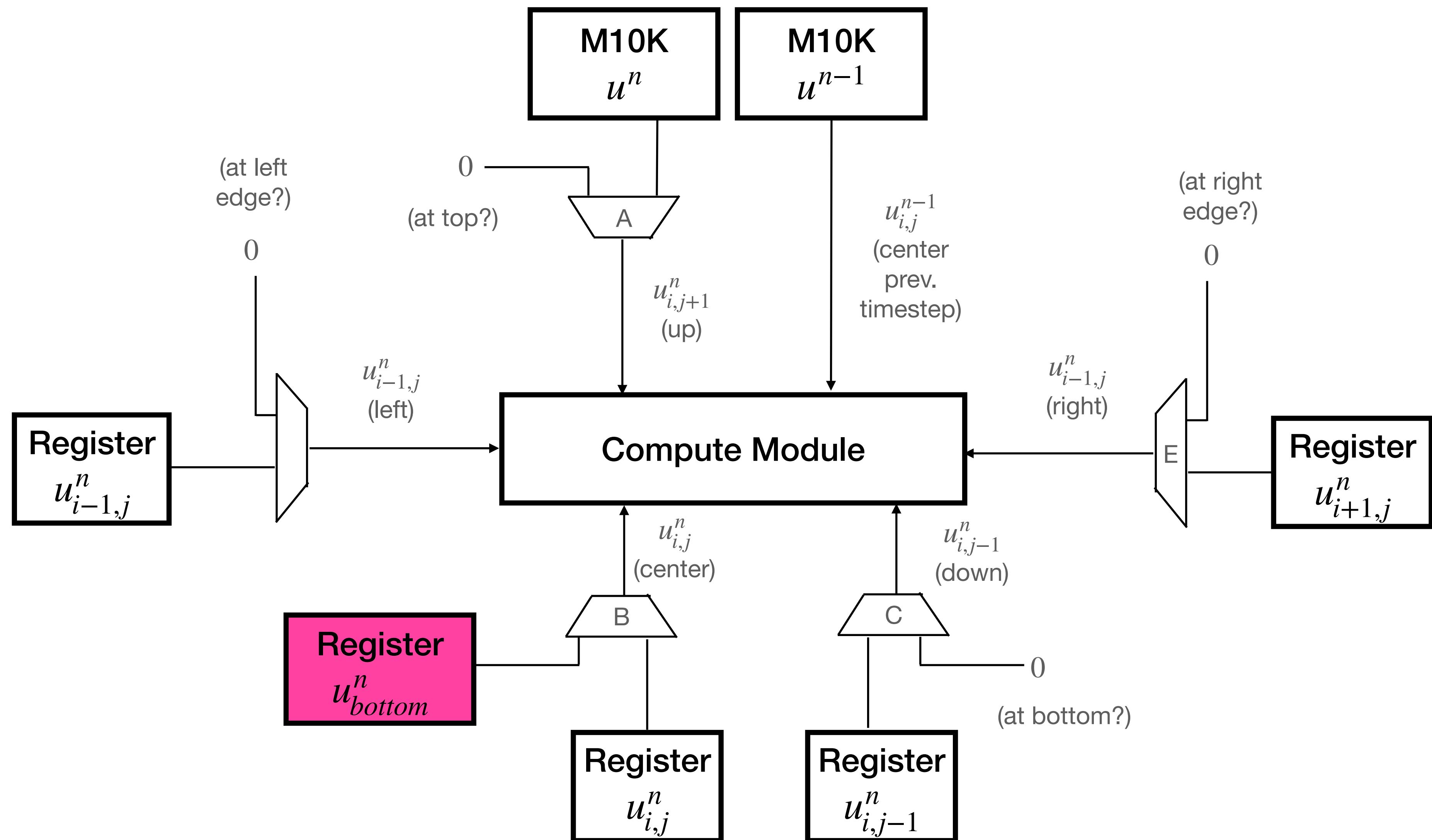
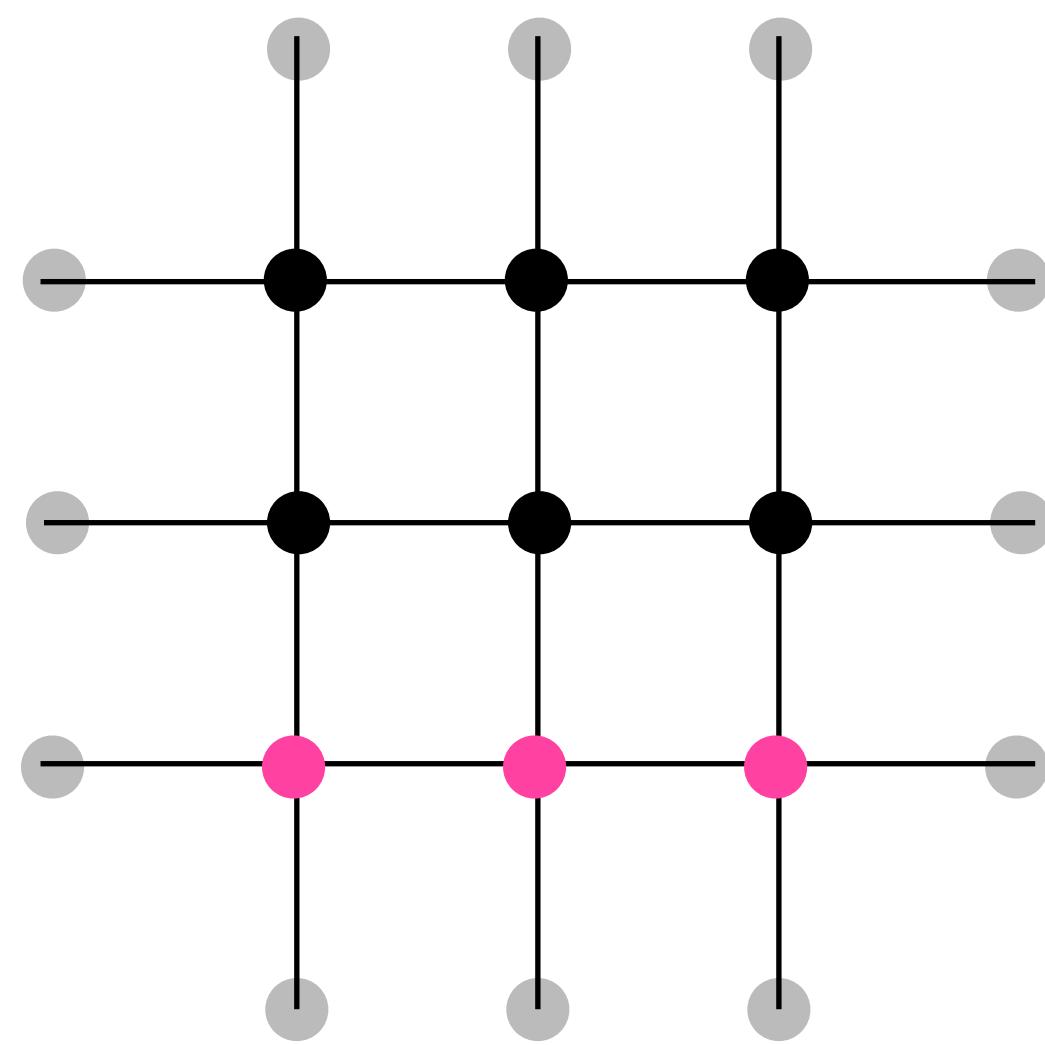
Initialize the  $n - 1$   
states of each node  
(write M10K memory)



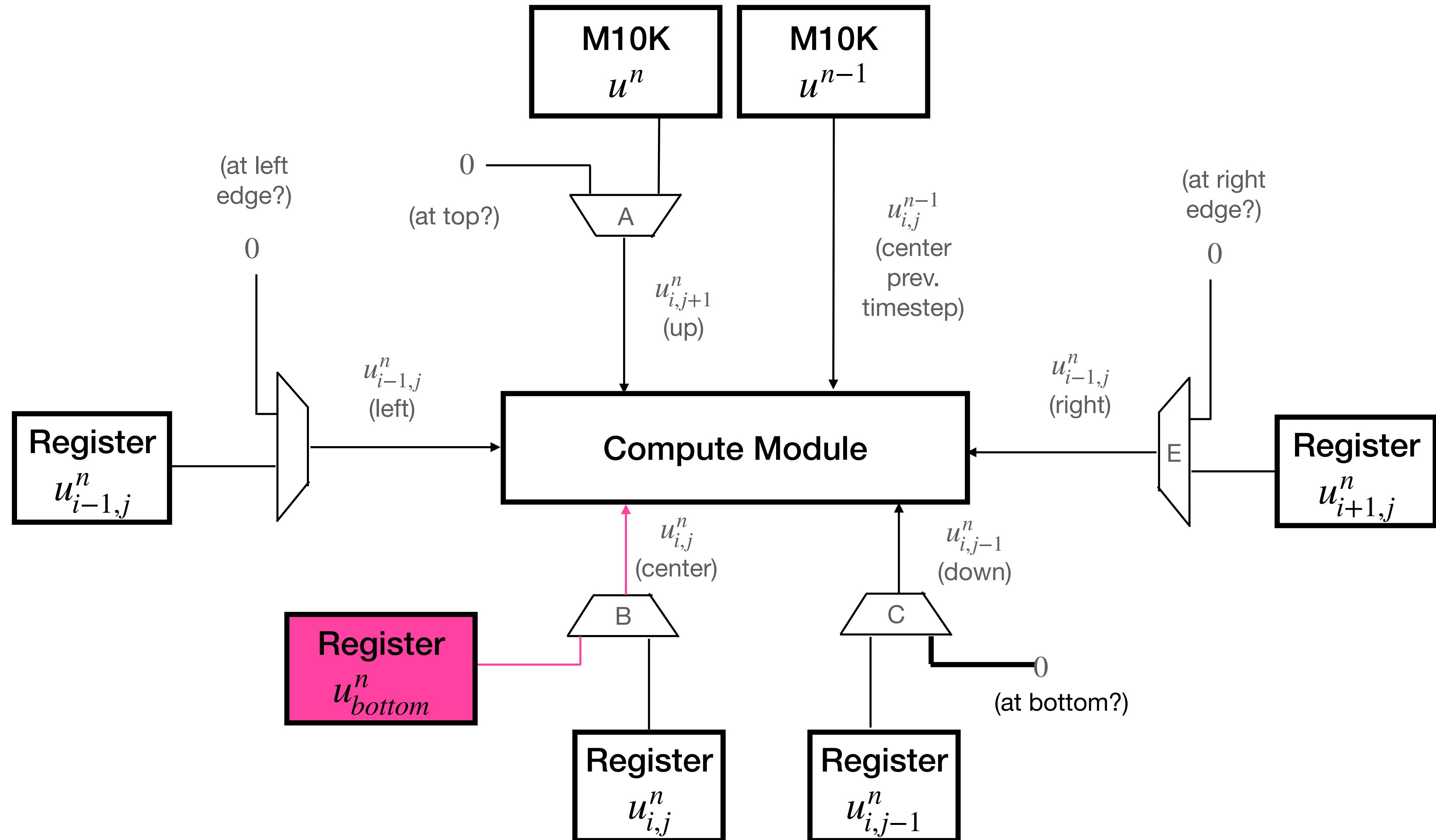
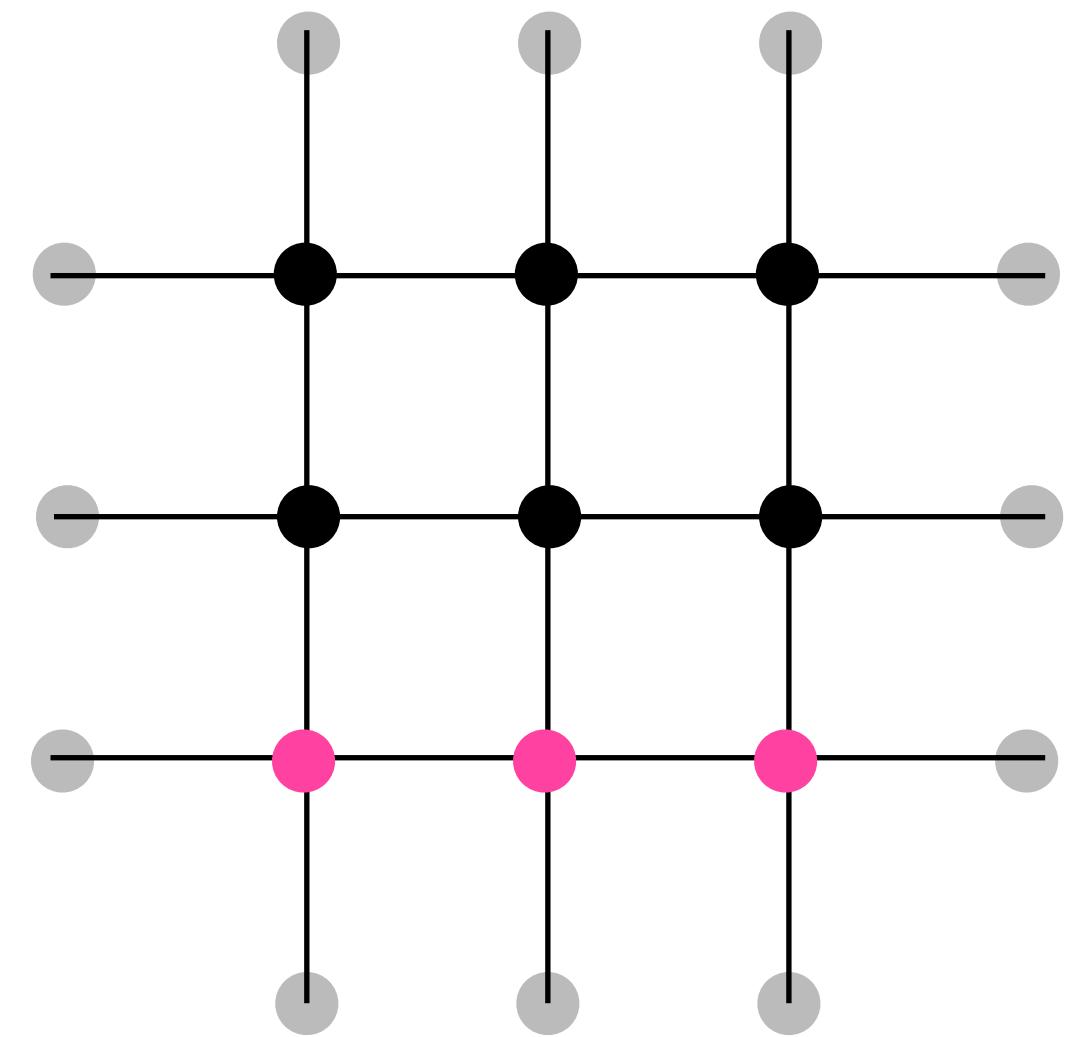
Initialize the  $n$  states  
of each node not in  
bottom row  
(write M10K memory)



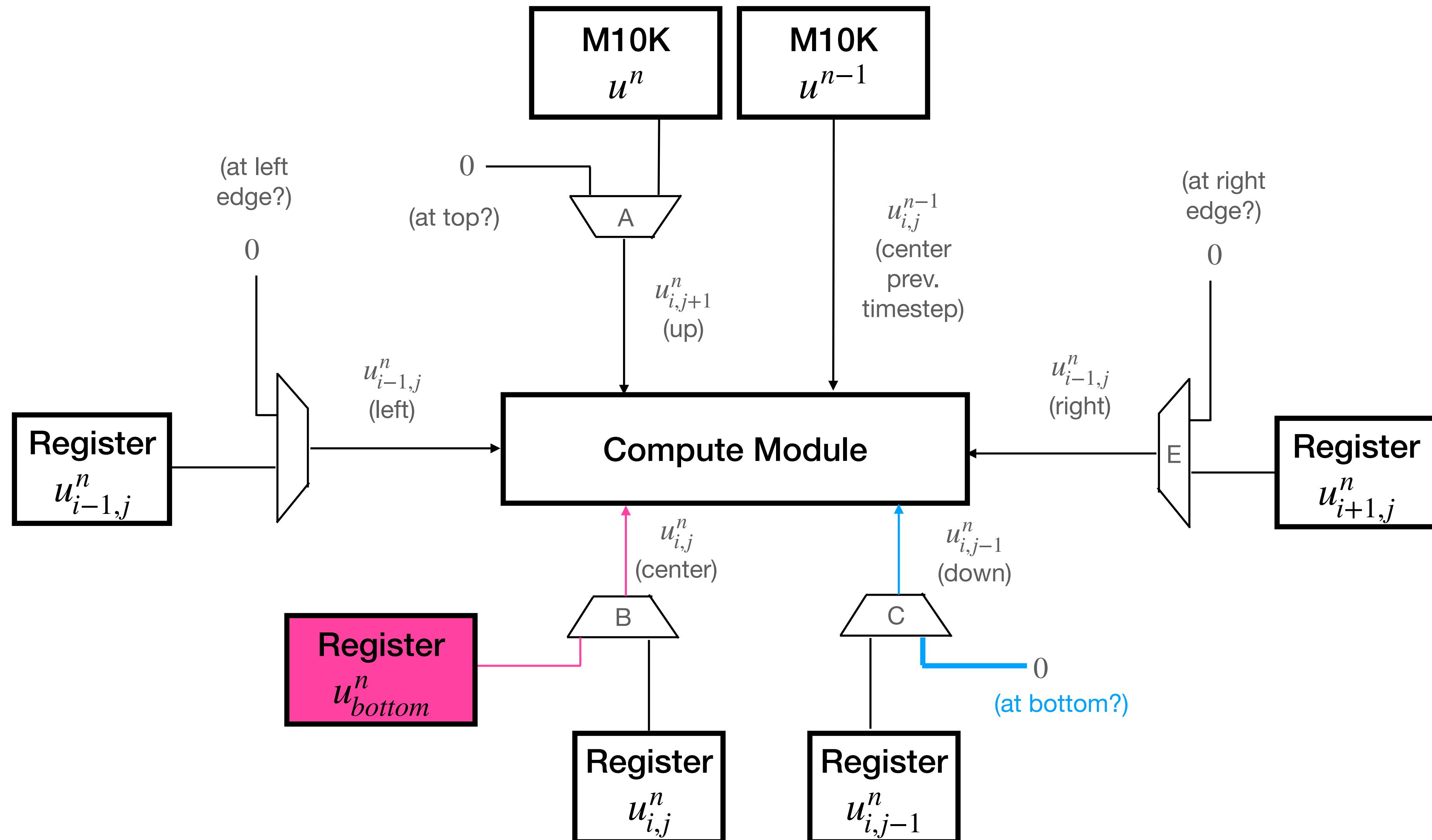
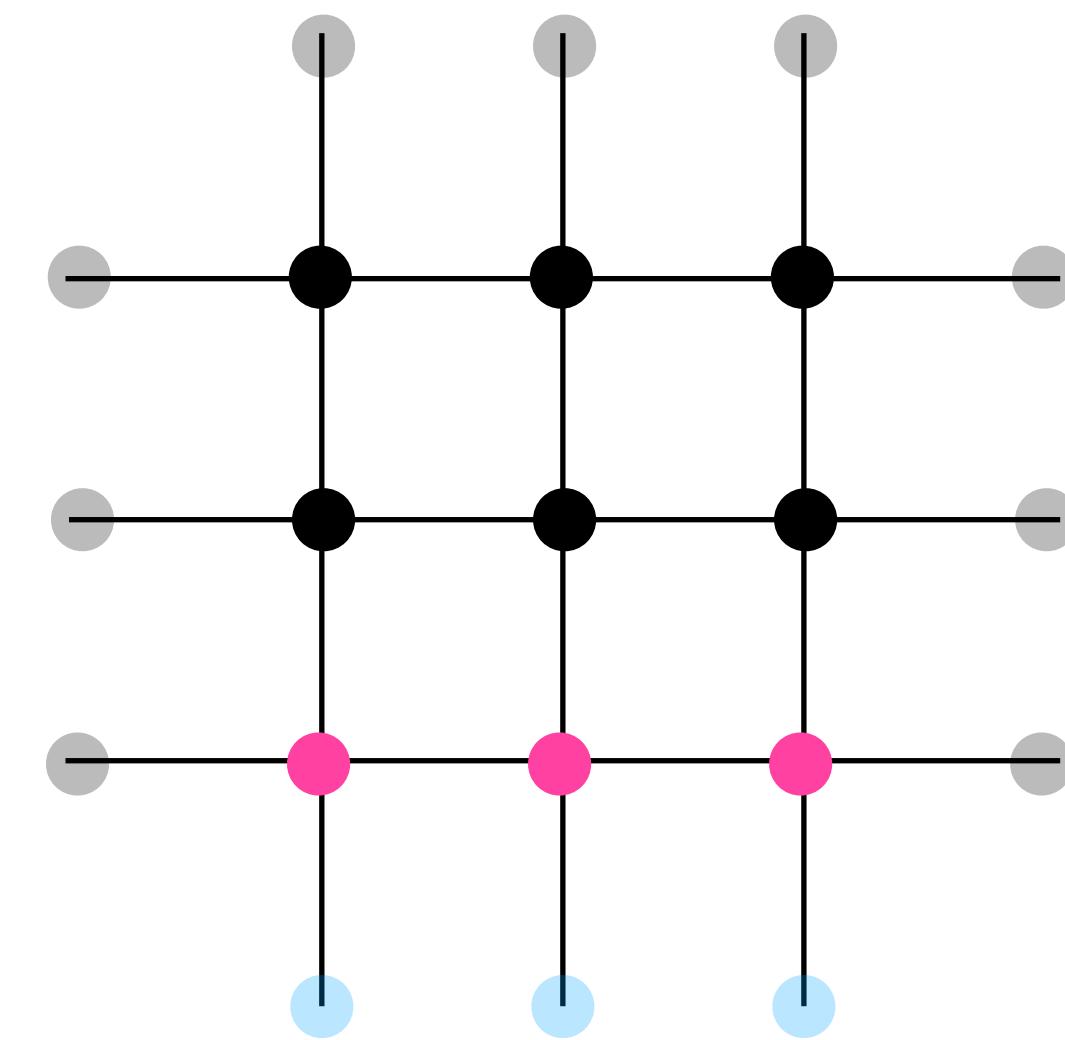
Initialize registers  
which hold the  
amplitudes of the  
bottom notes  $u_{bottom}^n$



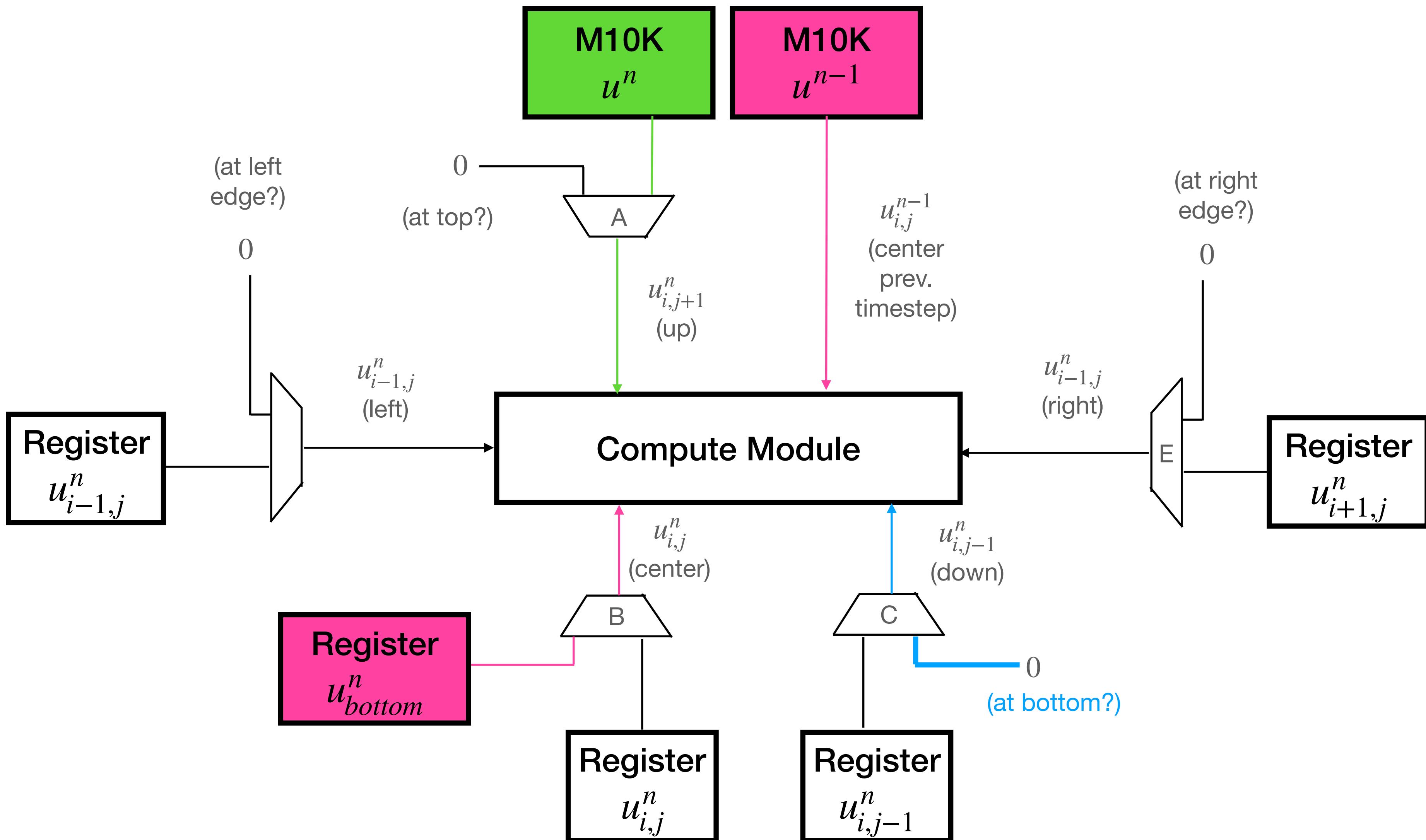
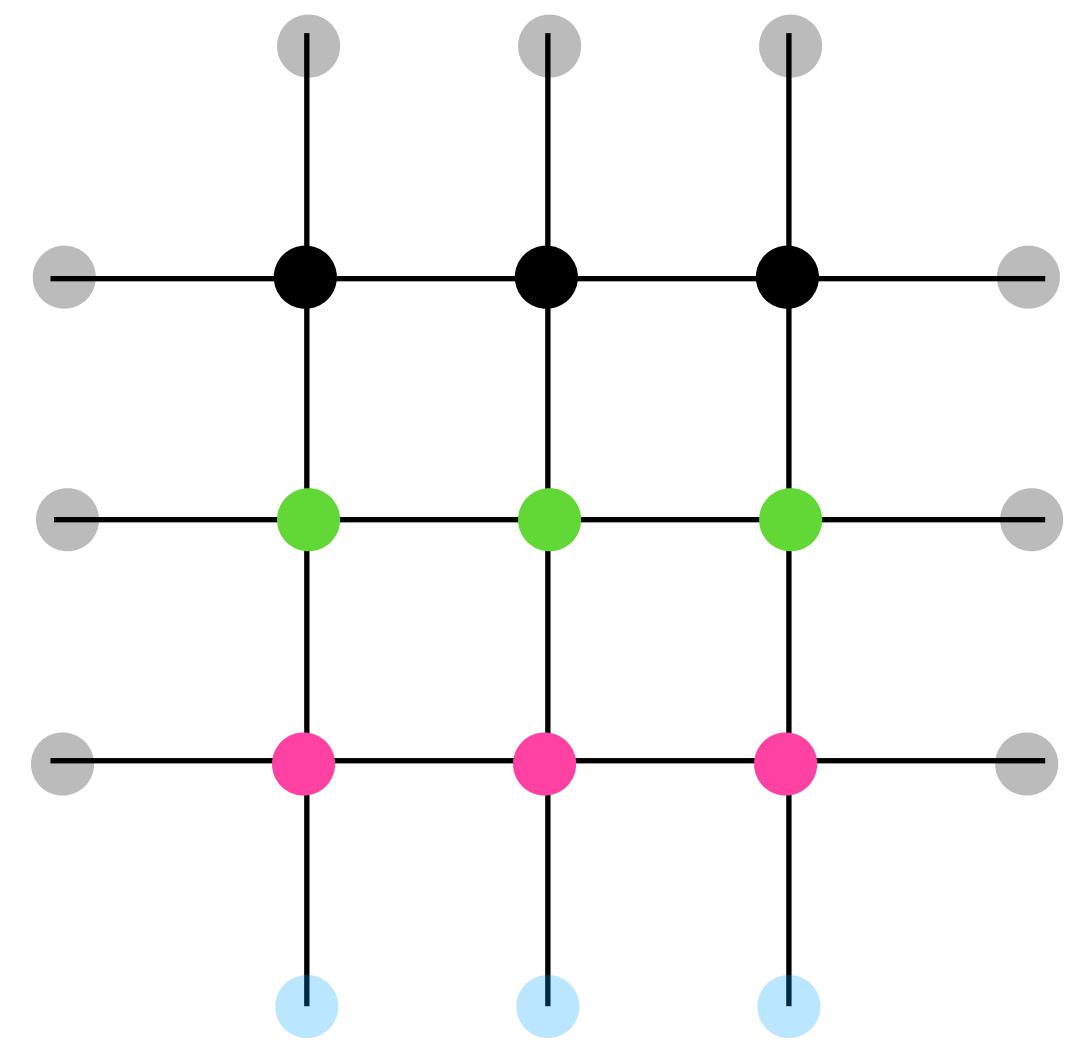
Start by updating the bottom row of the drum.



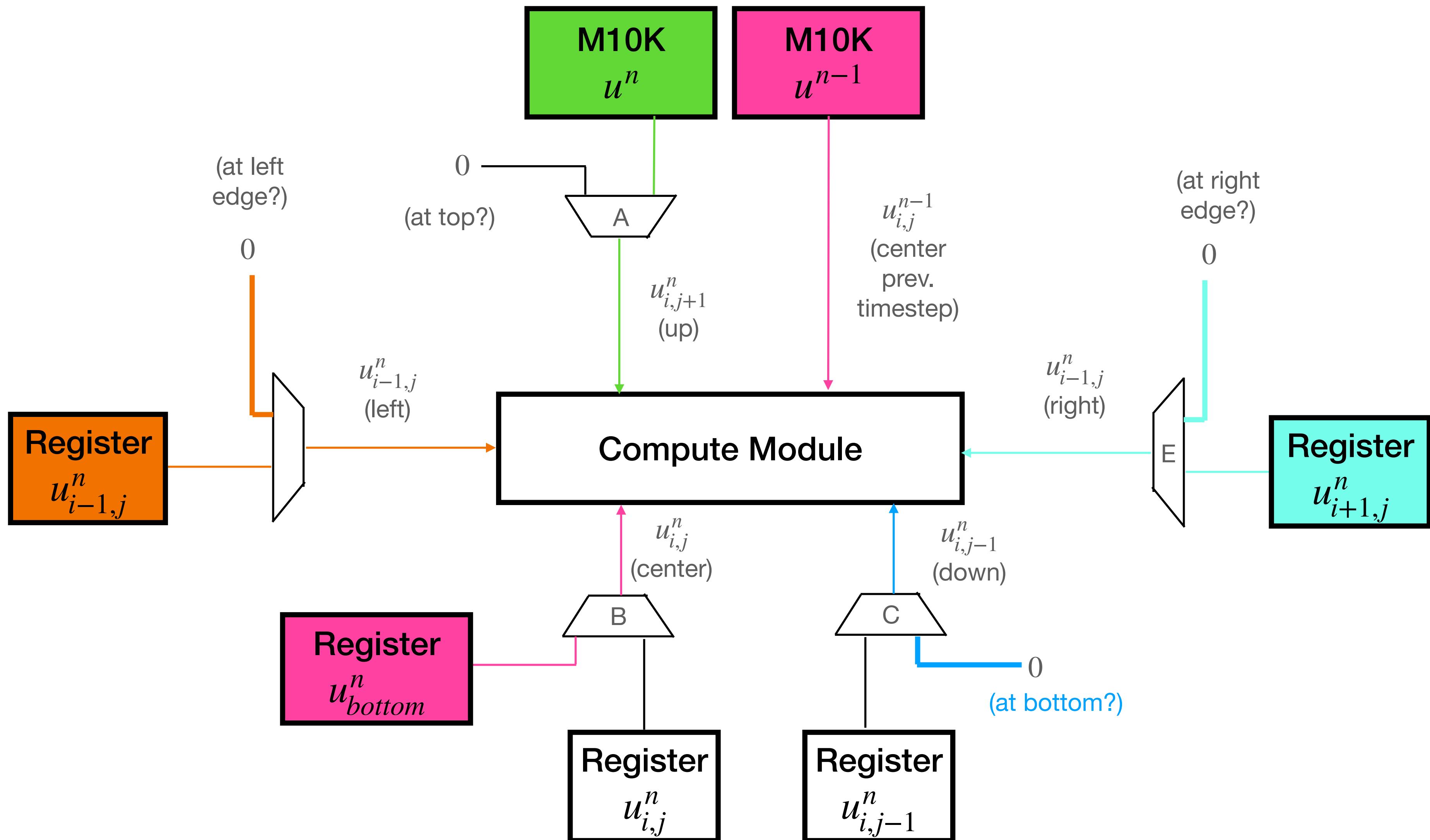
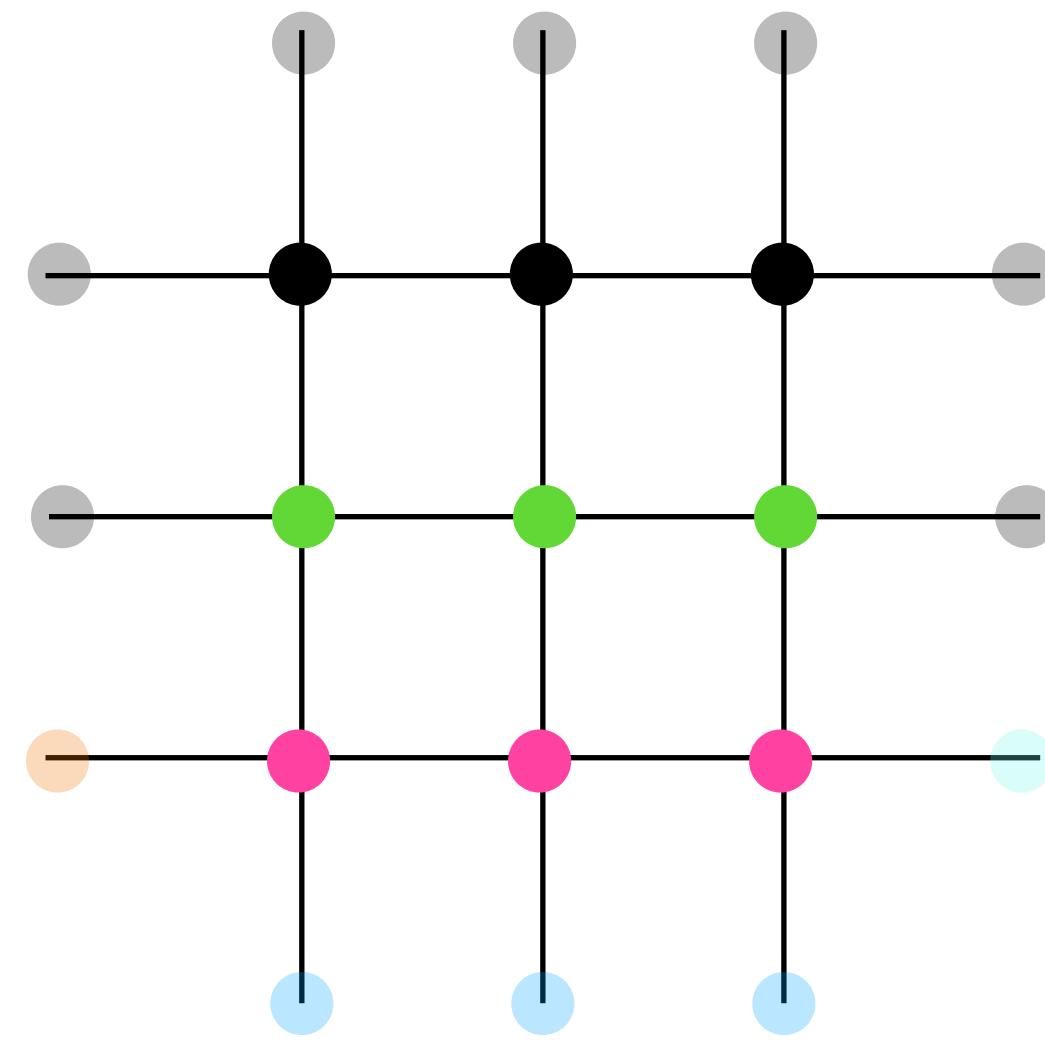
0 is multiplexed in for  
the “down” nodes  
since we are at an  
edge



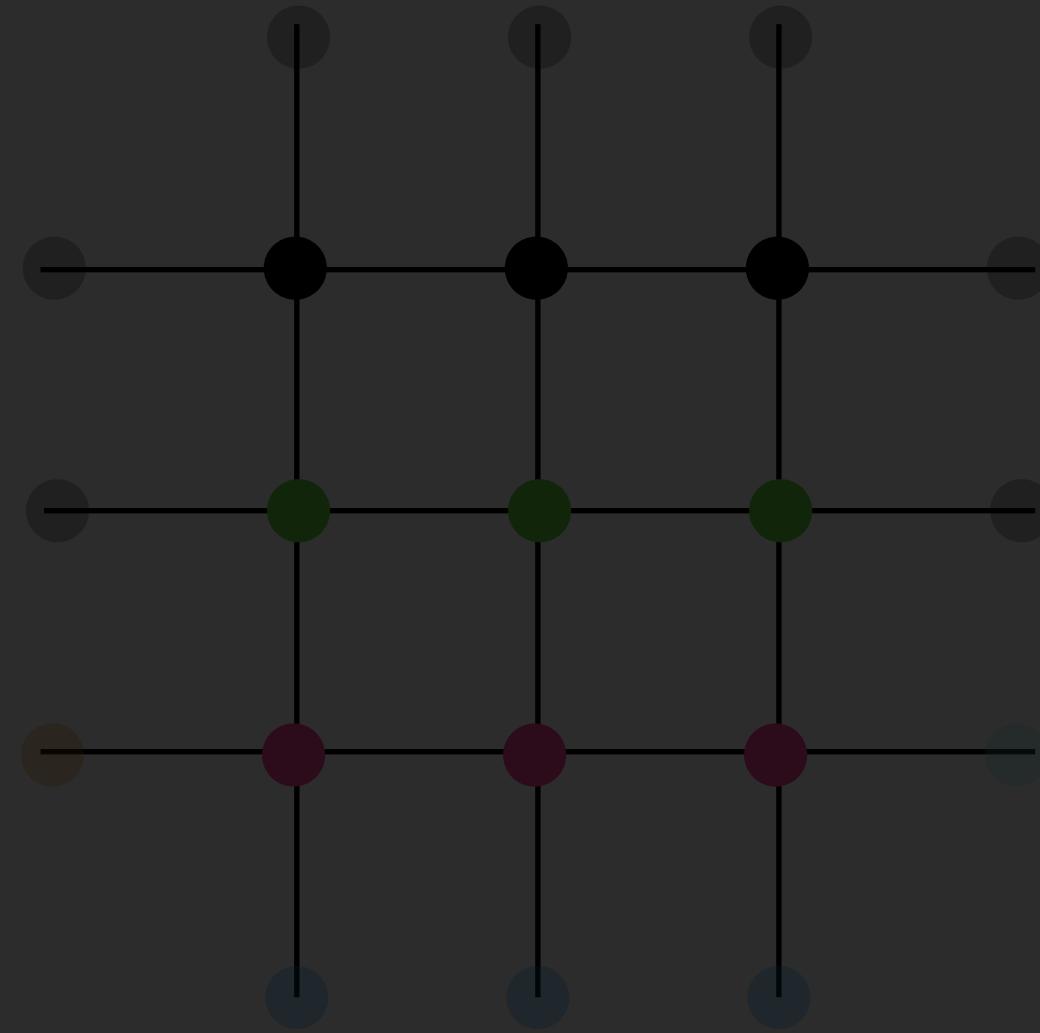
The “up” node and the  $n - 1$  state of center node are read from M10K memory



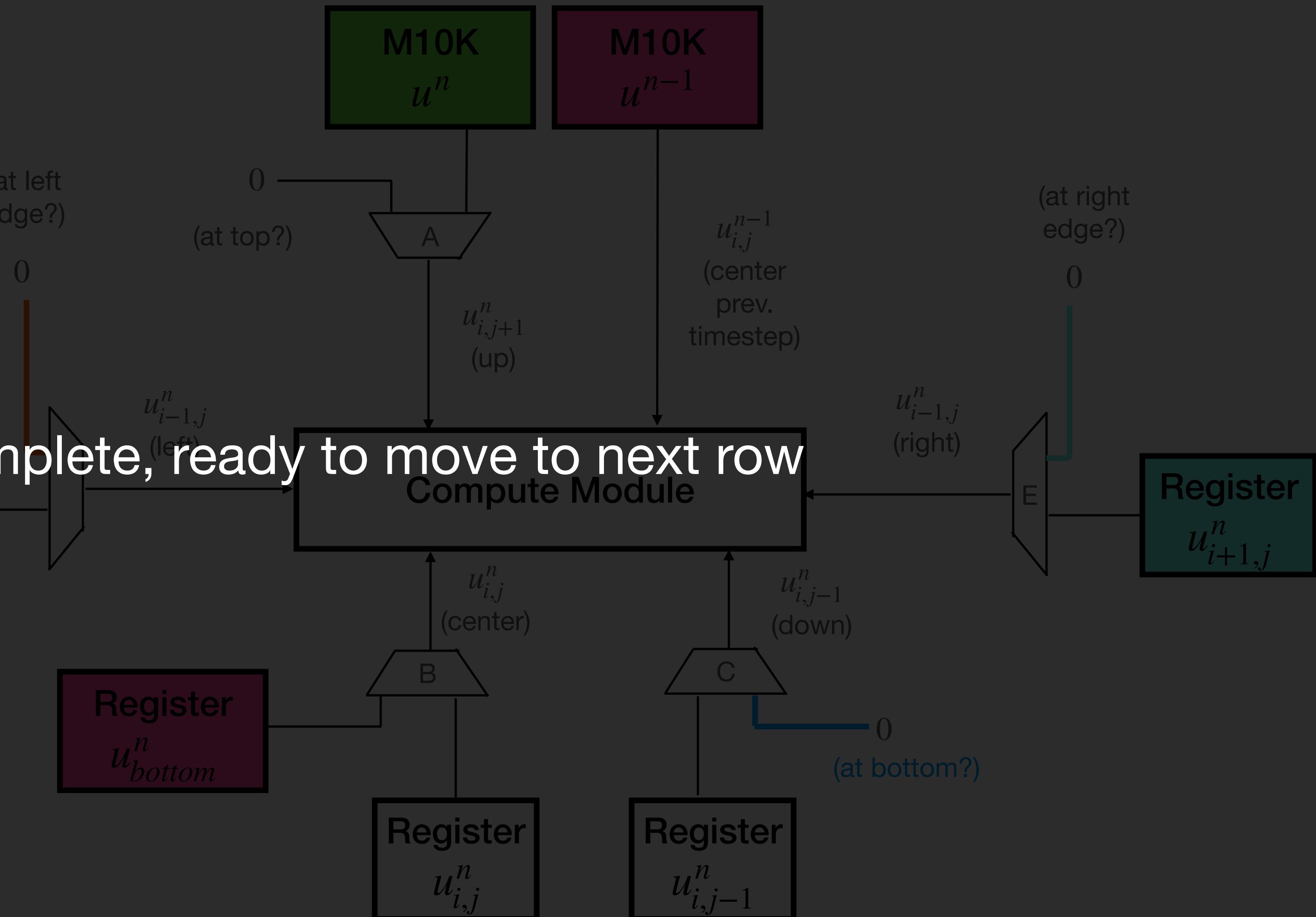
The “left” and “right” nodes are either the  $u_{bottom}^n$  registers from the adjacent columns, or 0

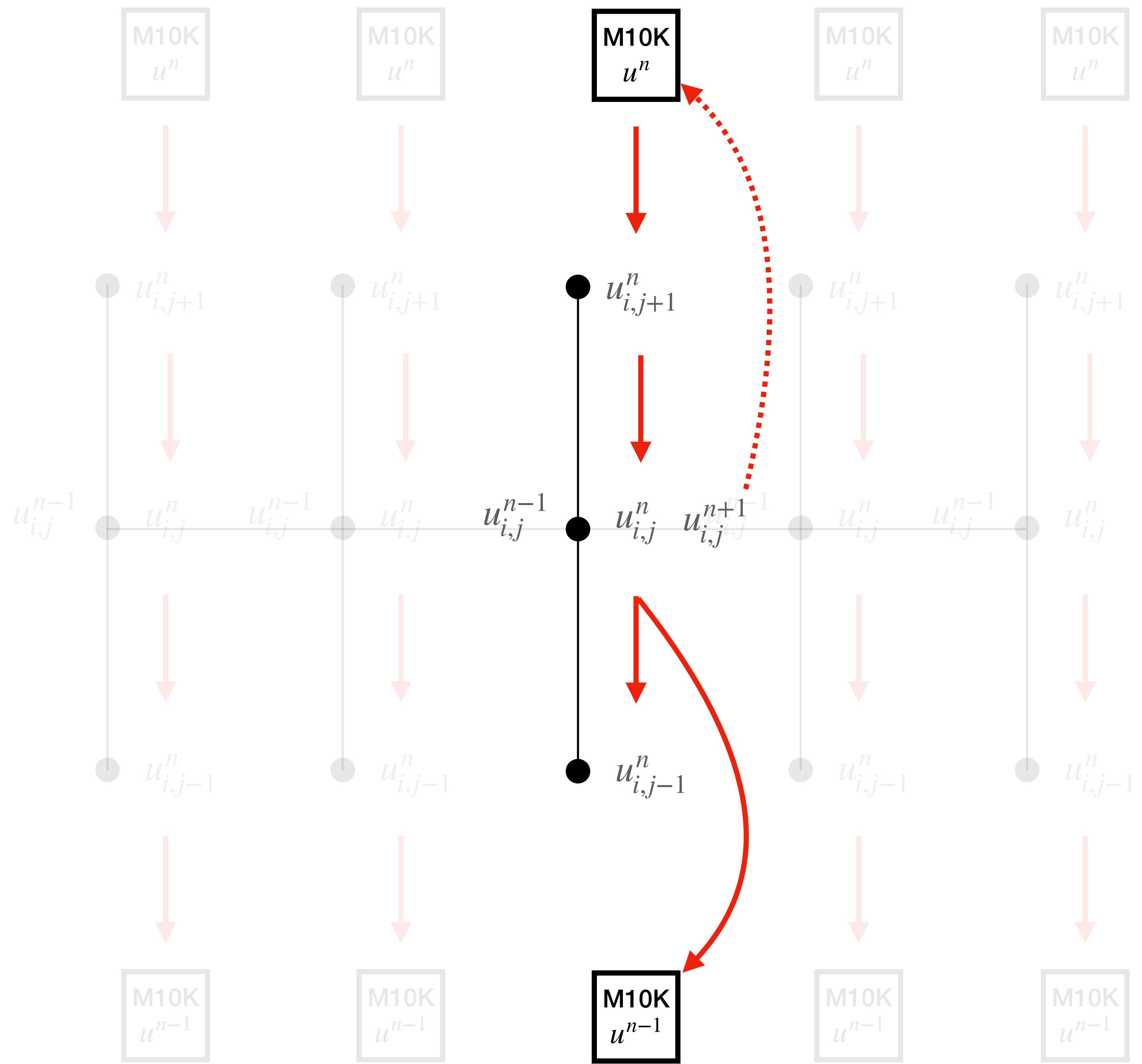


The “left” and “right” nodes are either the  $u_{bottom}^n$  registers from the adjacent columns, or 0



**Update complete, ready to move to next row**



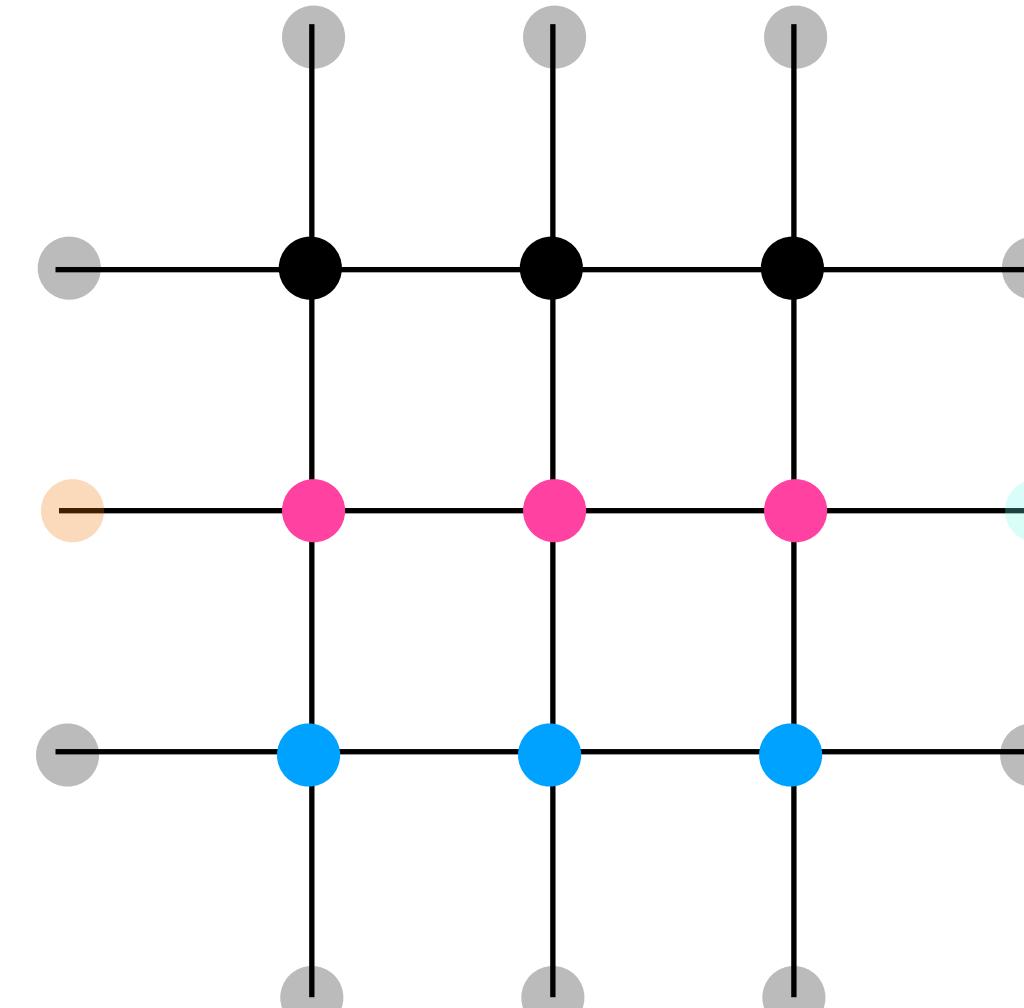


$$u_{bottom}^{n+1} \rightarrow u_{bottom}^n$$

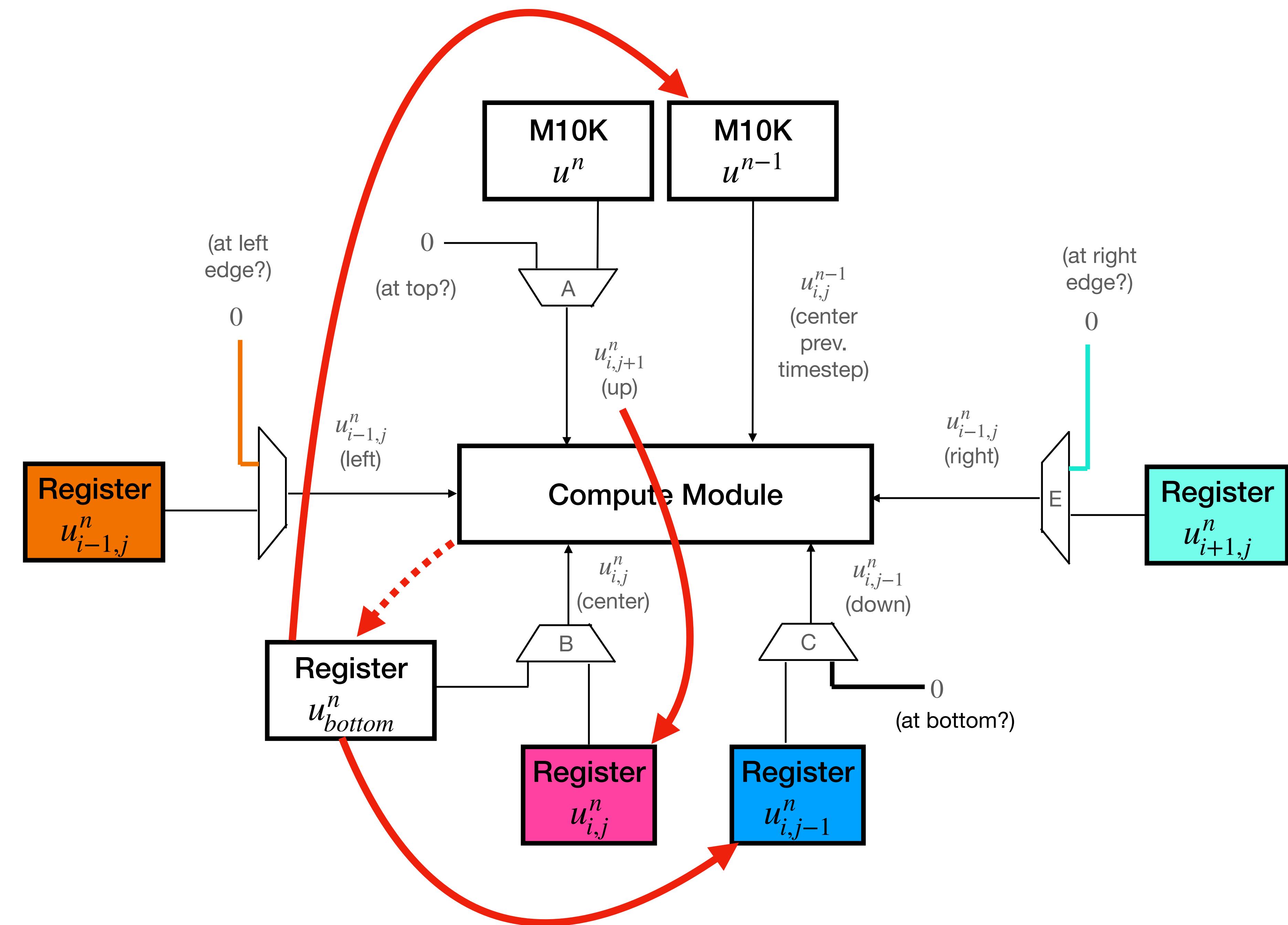
$$u_{bottom}^n \rightarrow u_{i,j-1}^n$$

$$u_{bottom}^n \rightarrow M10k\ n-1$$

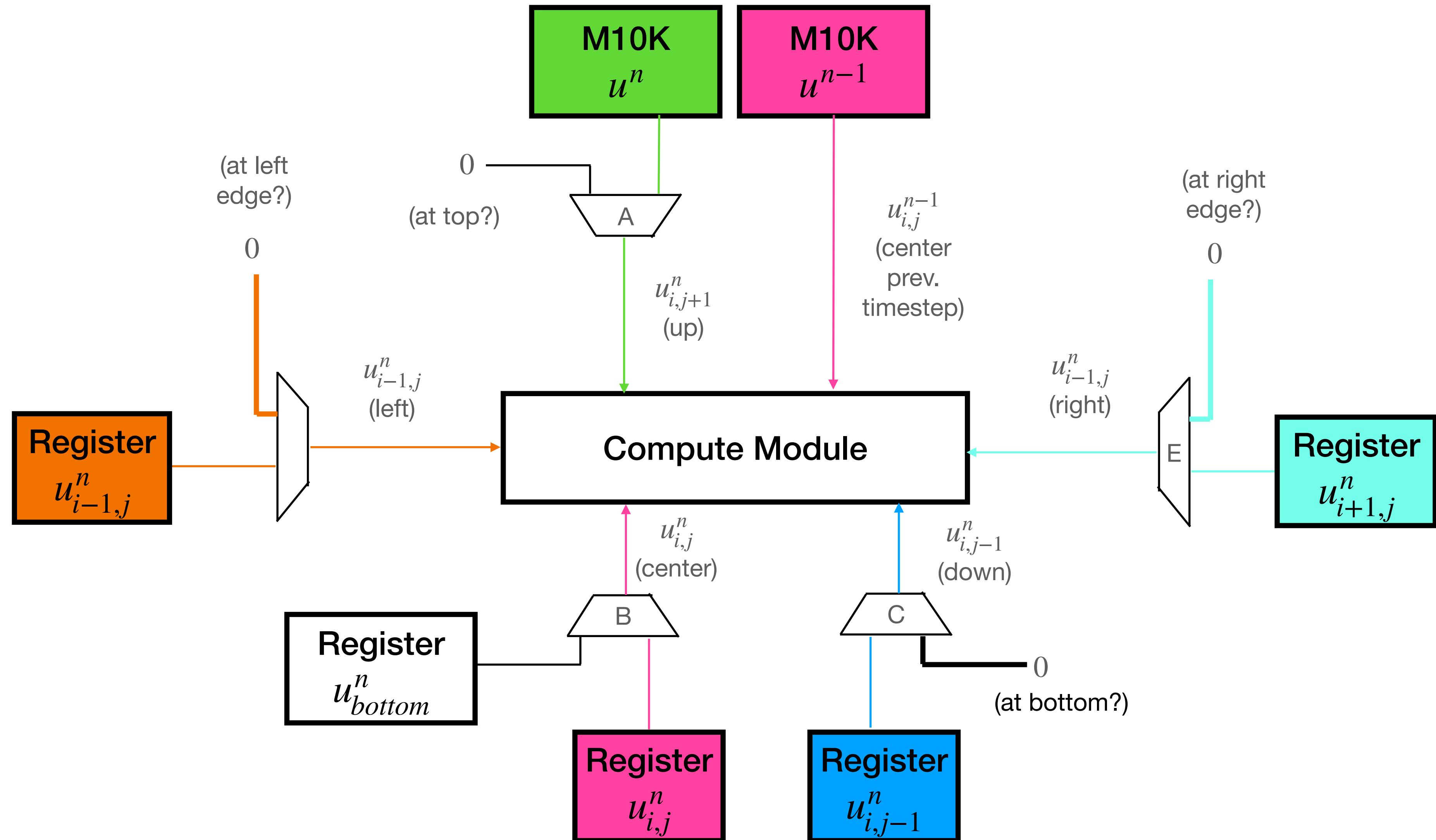
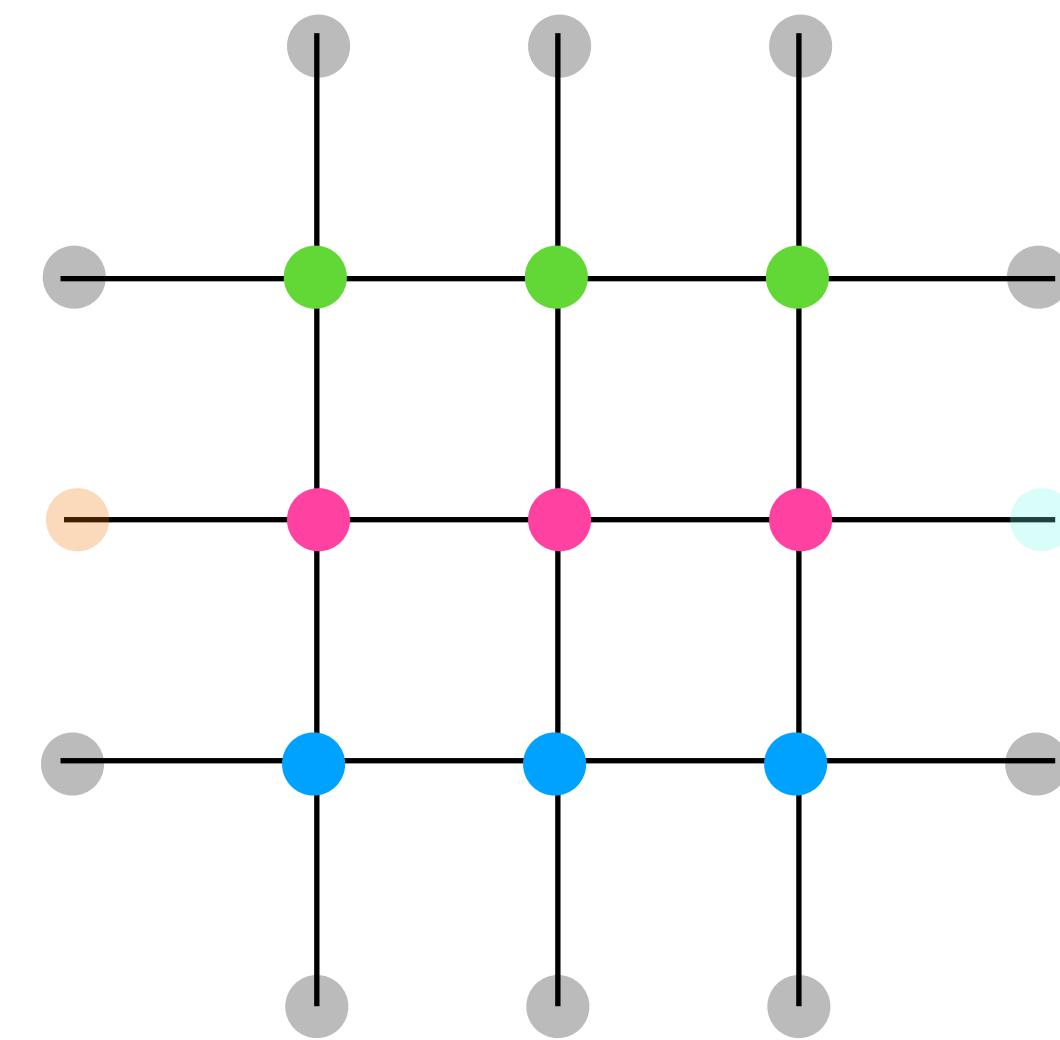
$$u_{i,j+1}^n \rightarrow u_{i,j}^n$$



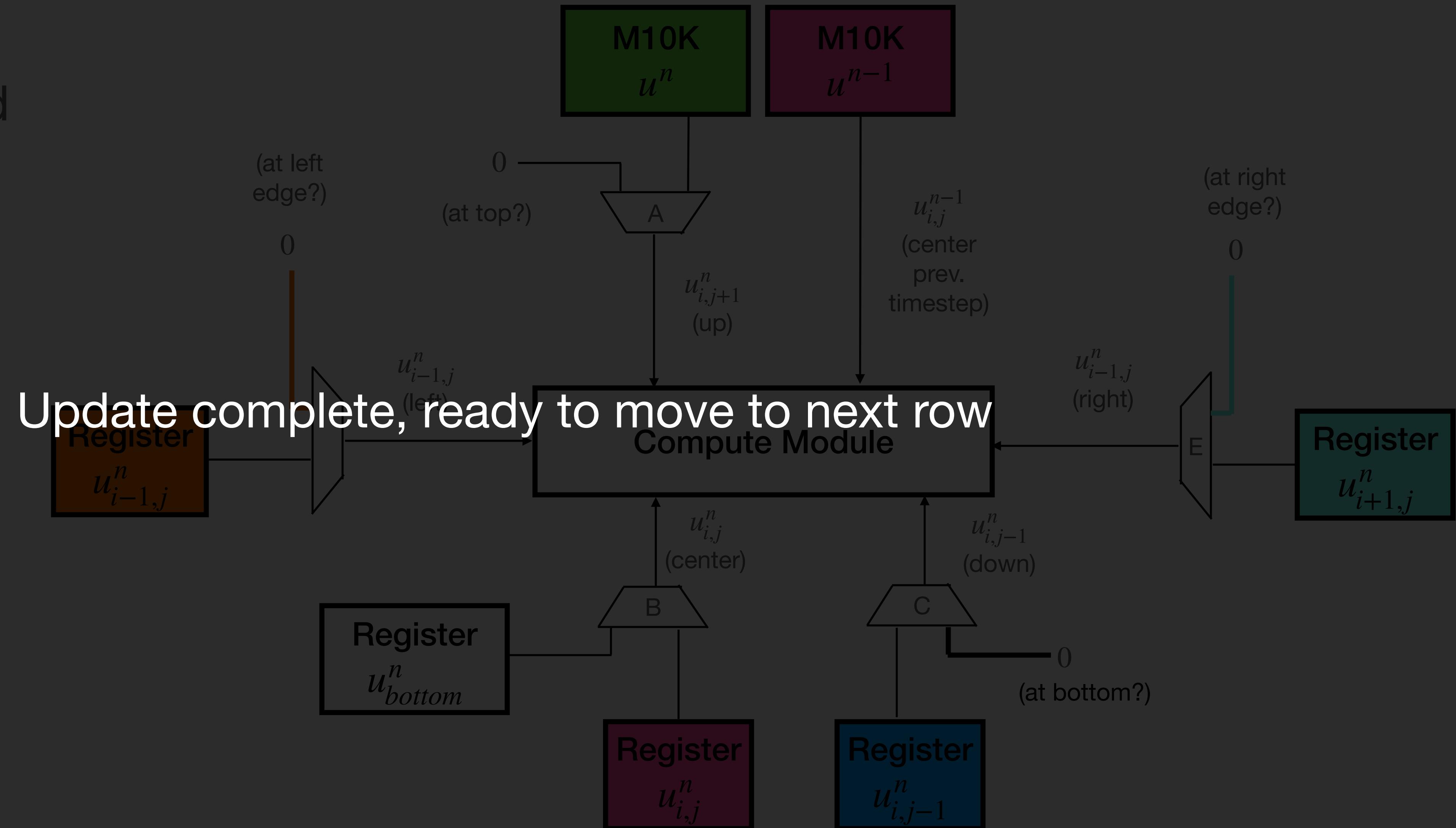
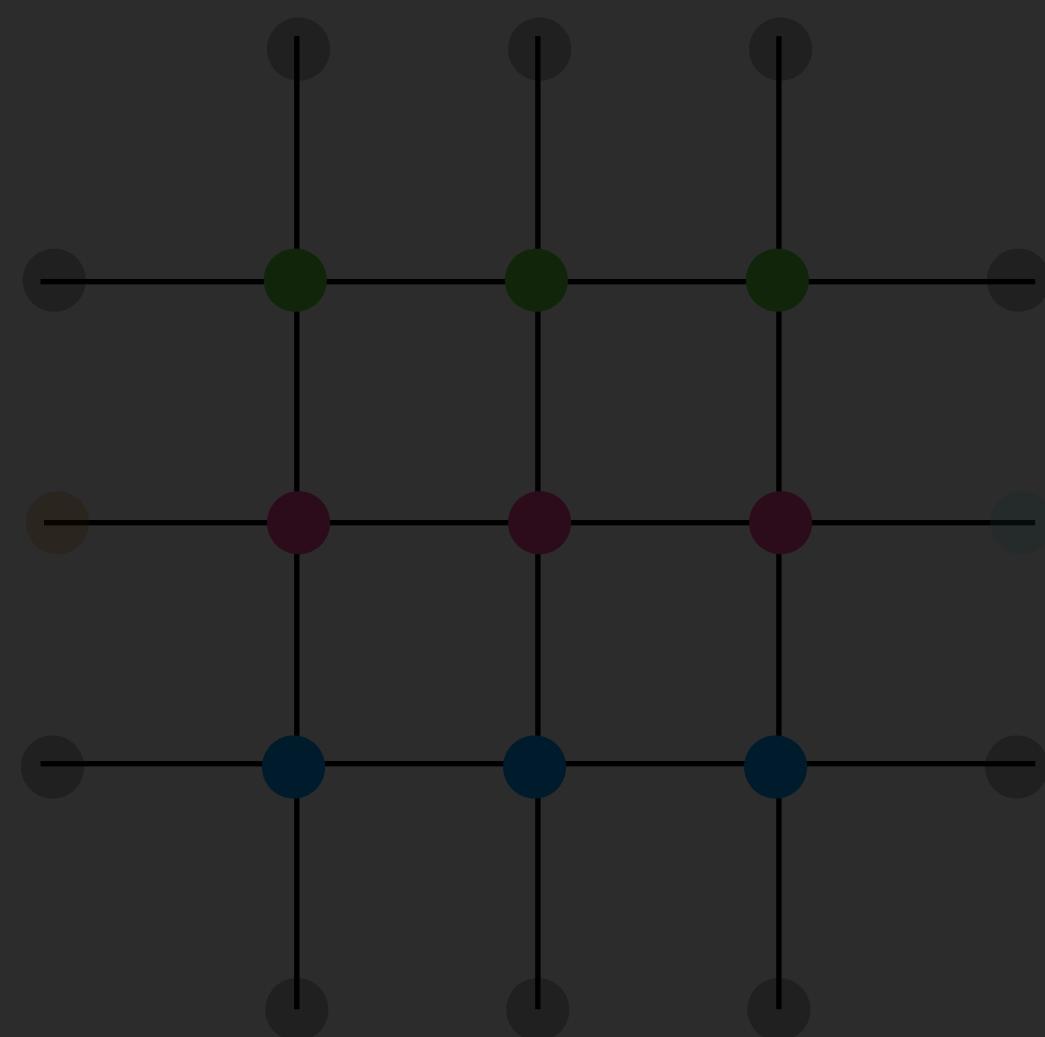
(happens in parallel across all columns, so left/right values update when each column updates)



The “up” node and the  $n - 1$  state of center node are read from M10K memory



The “up” node and the  $n - 1$  state of center node are read from M10K memory

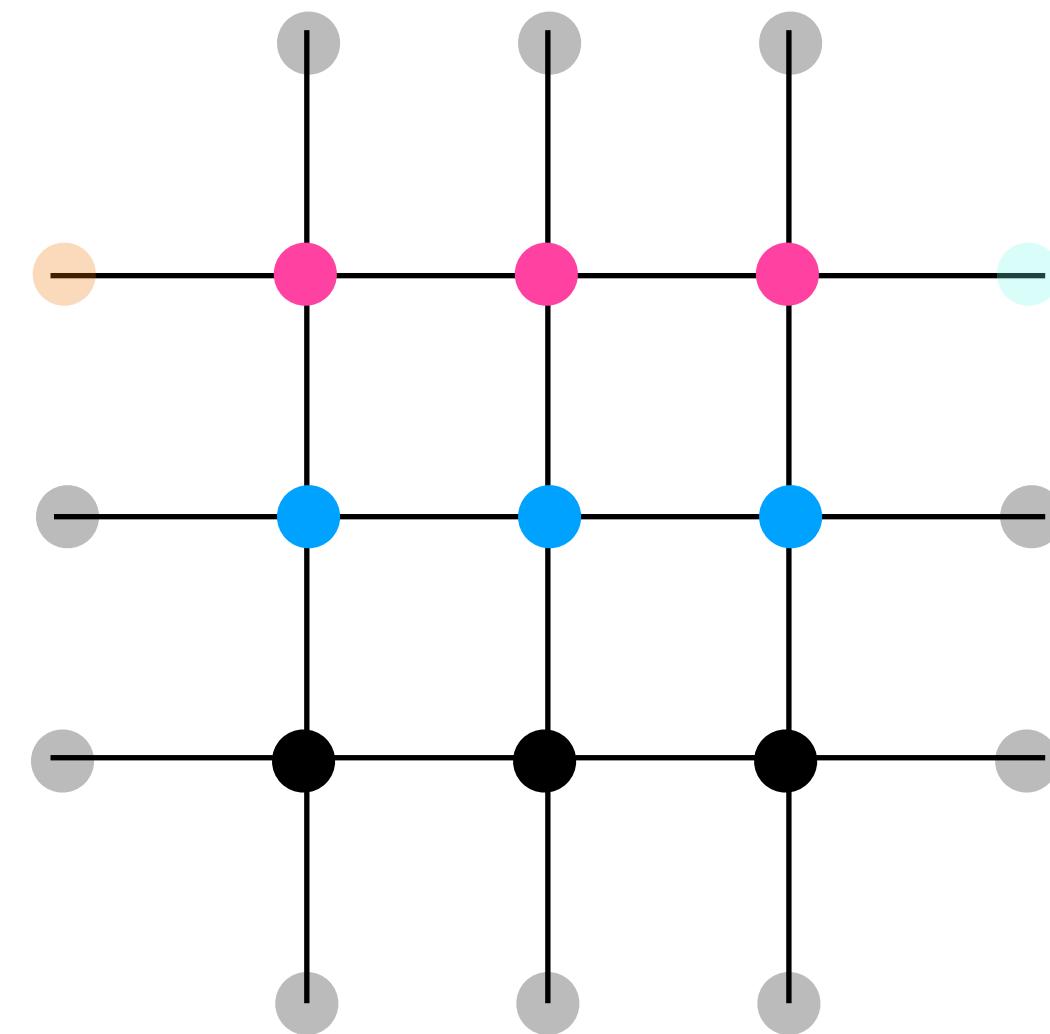


$$u_{i,j}^{n+1} \rightarrow \text{M10k } n$$

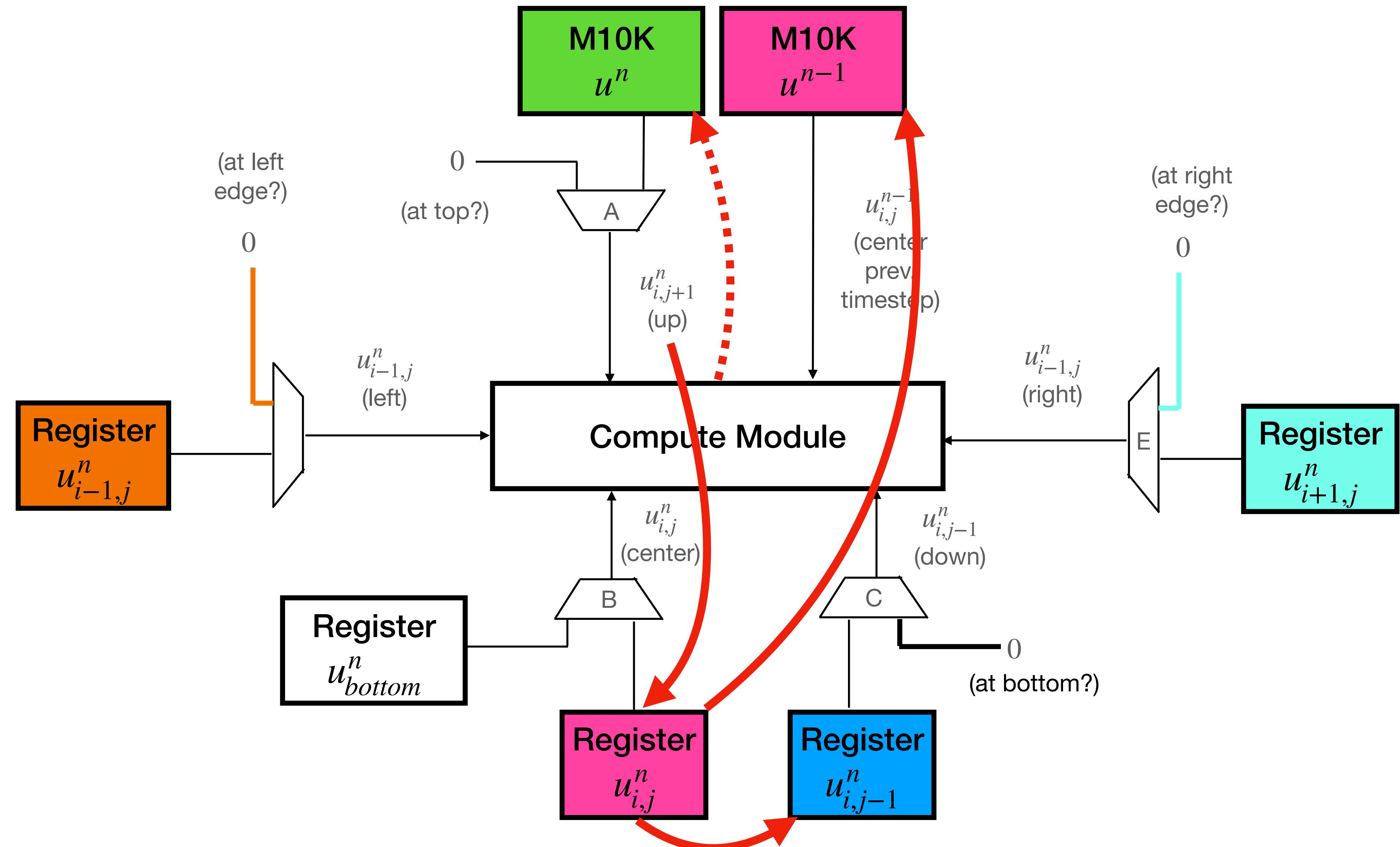
$$u_{i,j+1}^n \rightarrow u_{i,j}^n$$

$$u_{i,j}^n \rightarrow u_{i,j-1}^n$$

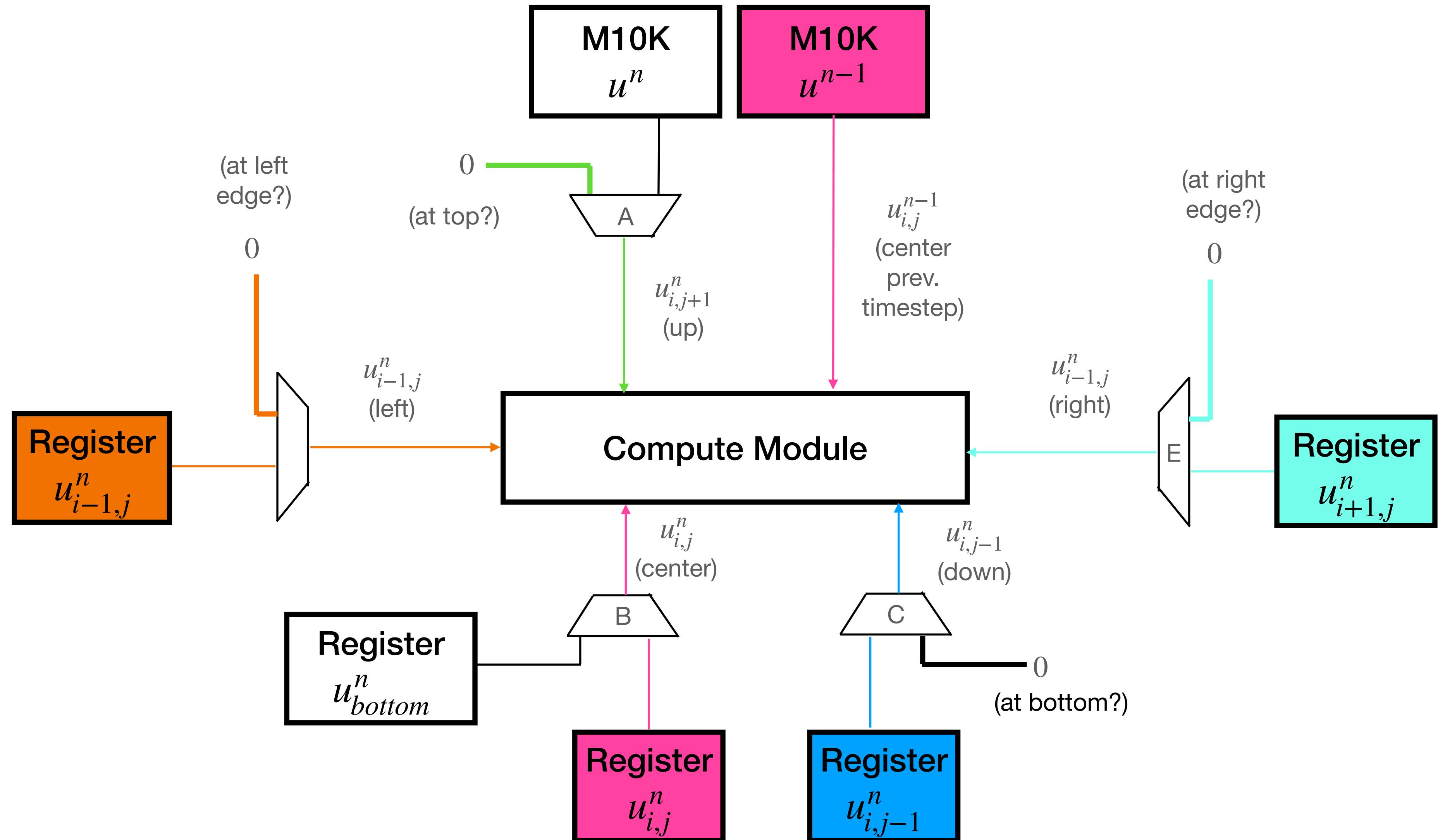
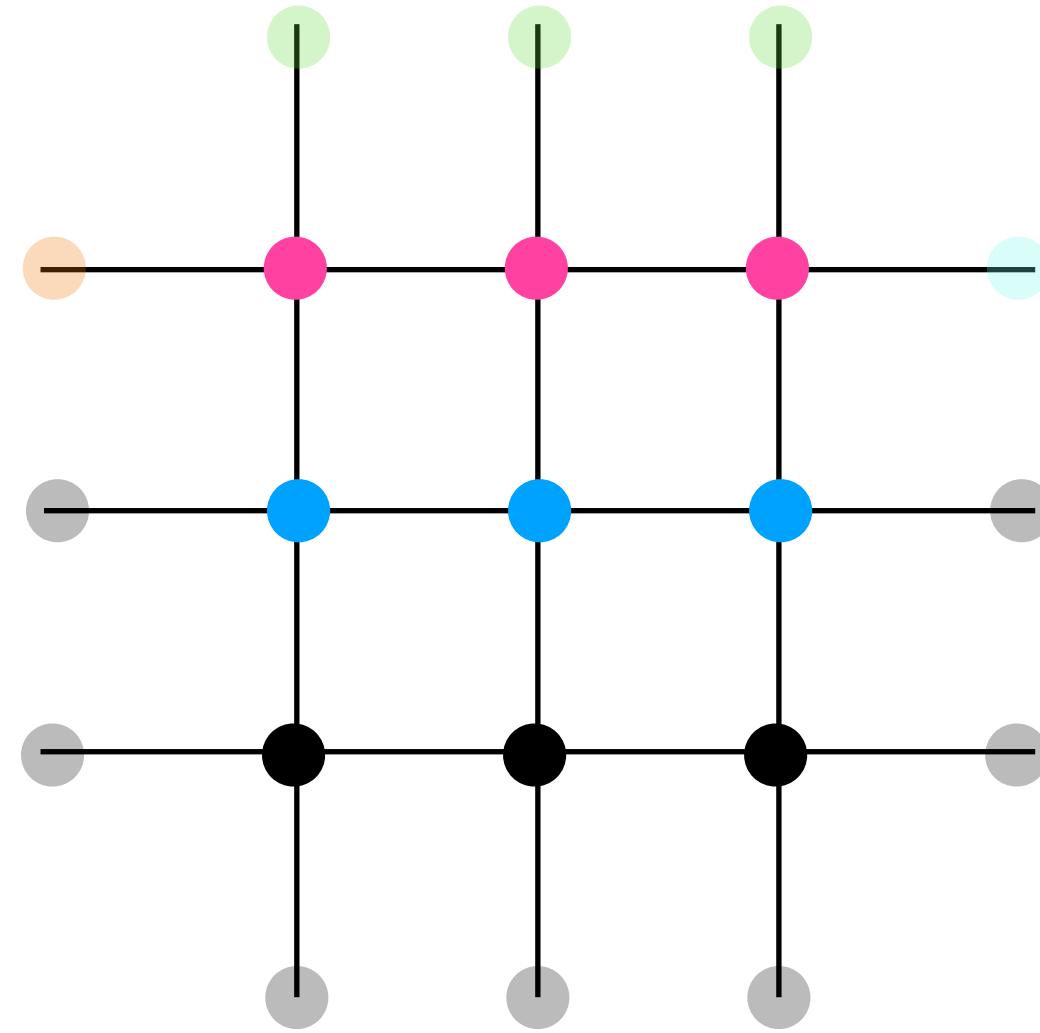
$$u_{i,j-1}^n \rightarrow \text{M10k } n-1$$



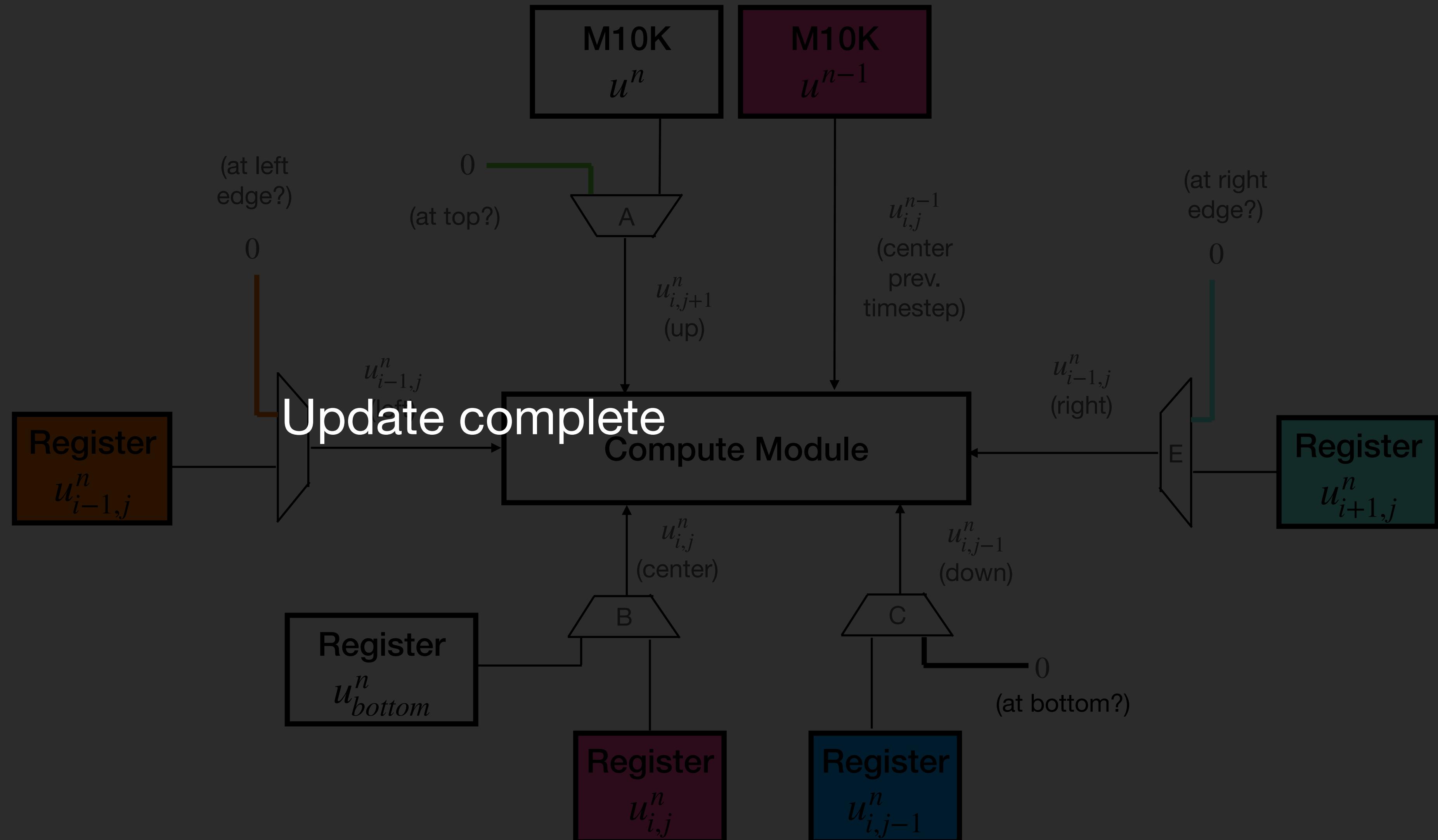
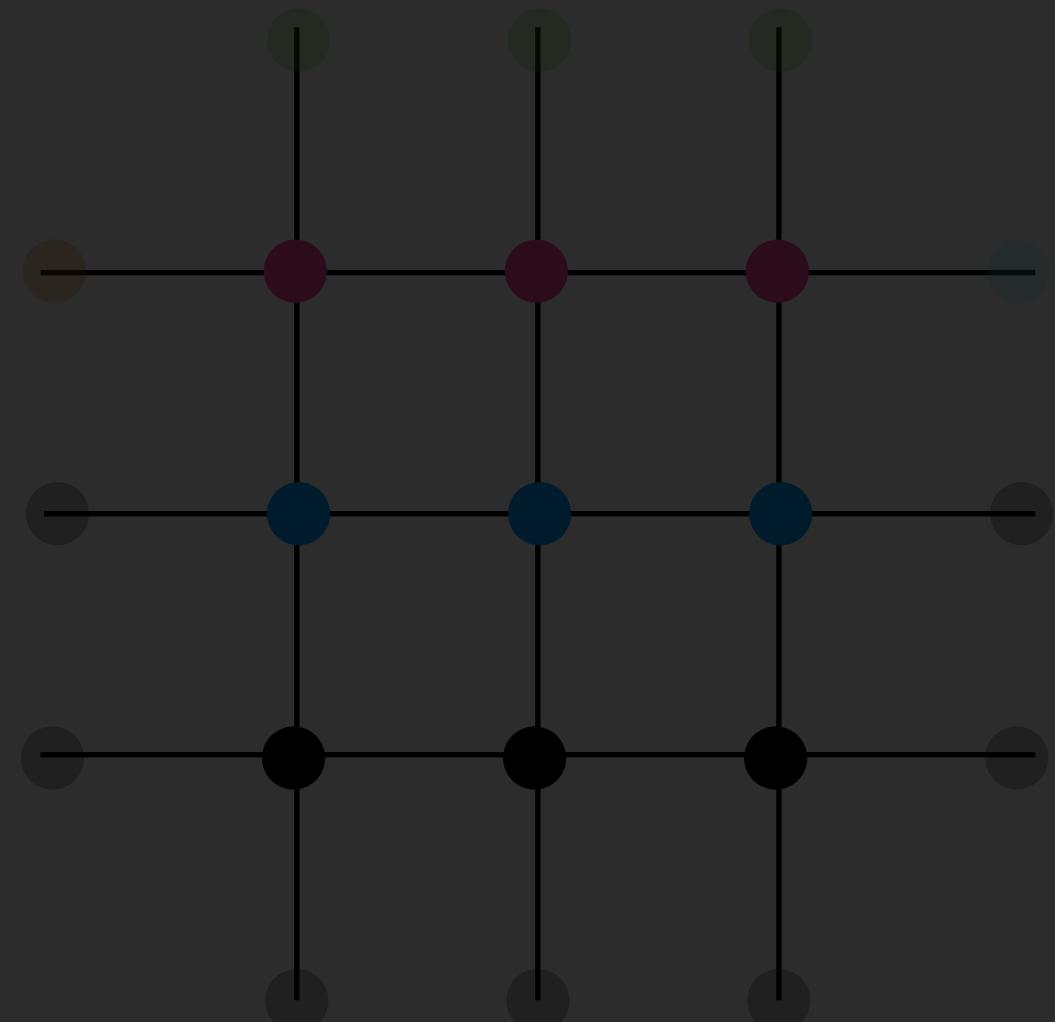
This is how information moves for *most* of the rows of the drum. The only other special-case row is the top

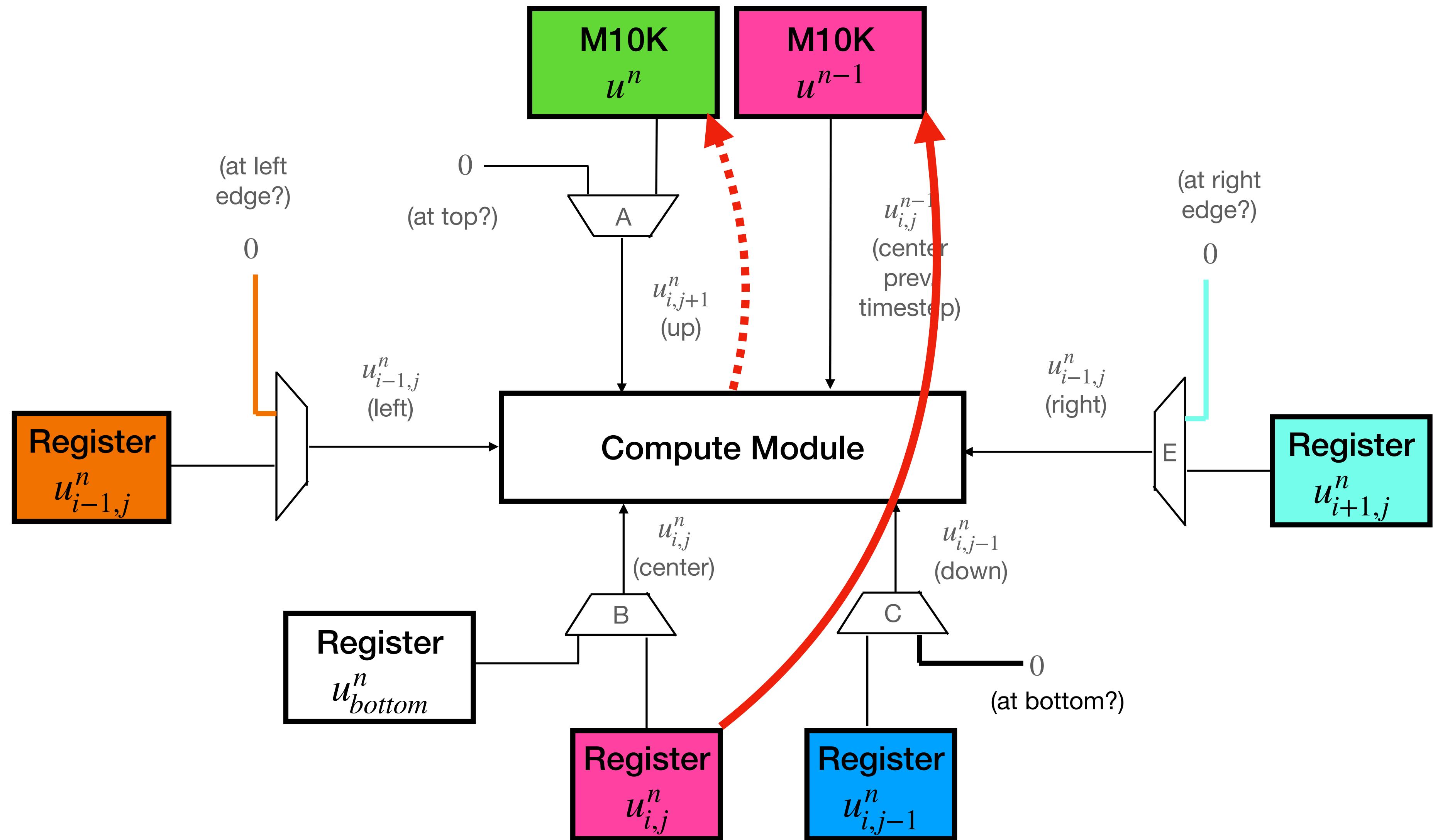
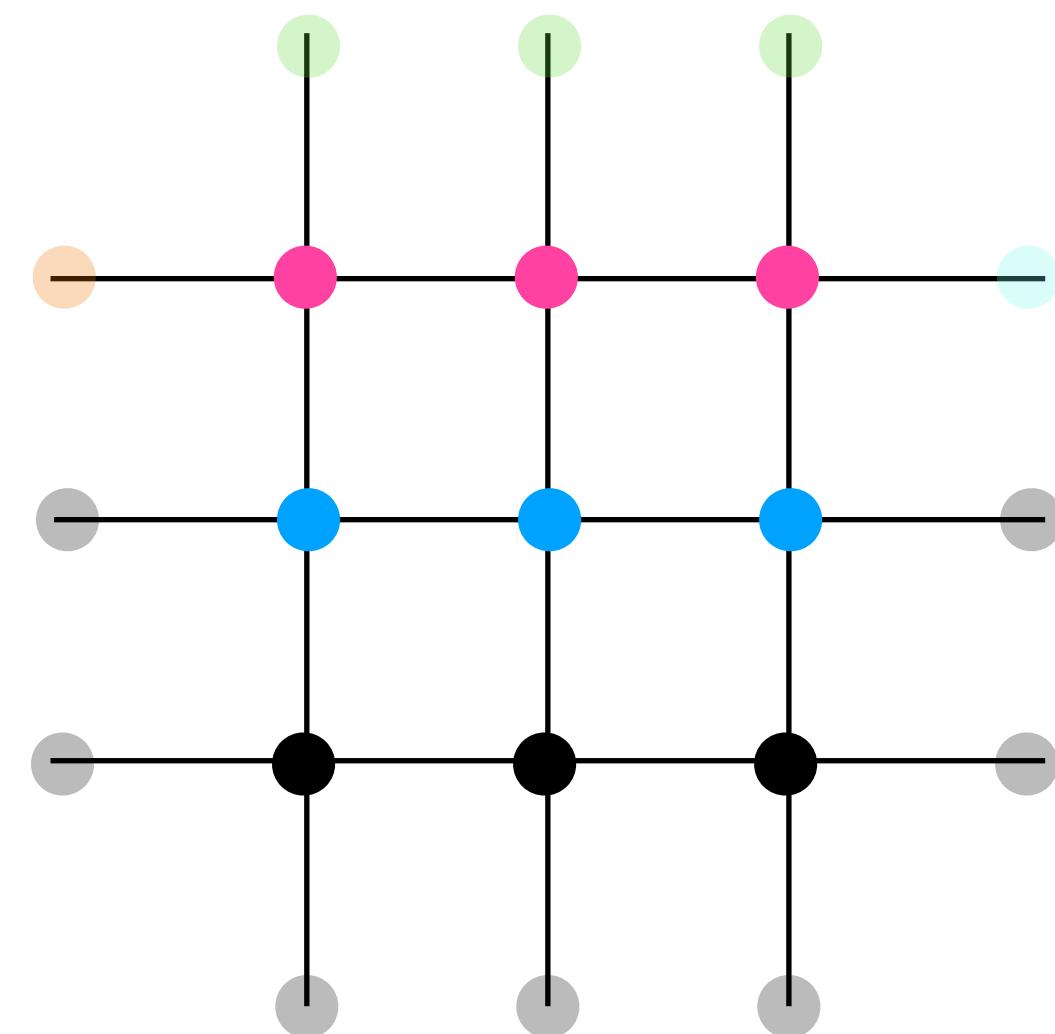


0 is multiplexed in for  
the “up node, the  
 $n - 1$  state of center  
node is read from  
M10K memory



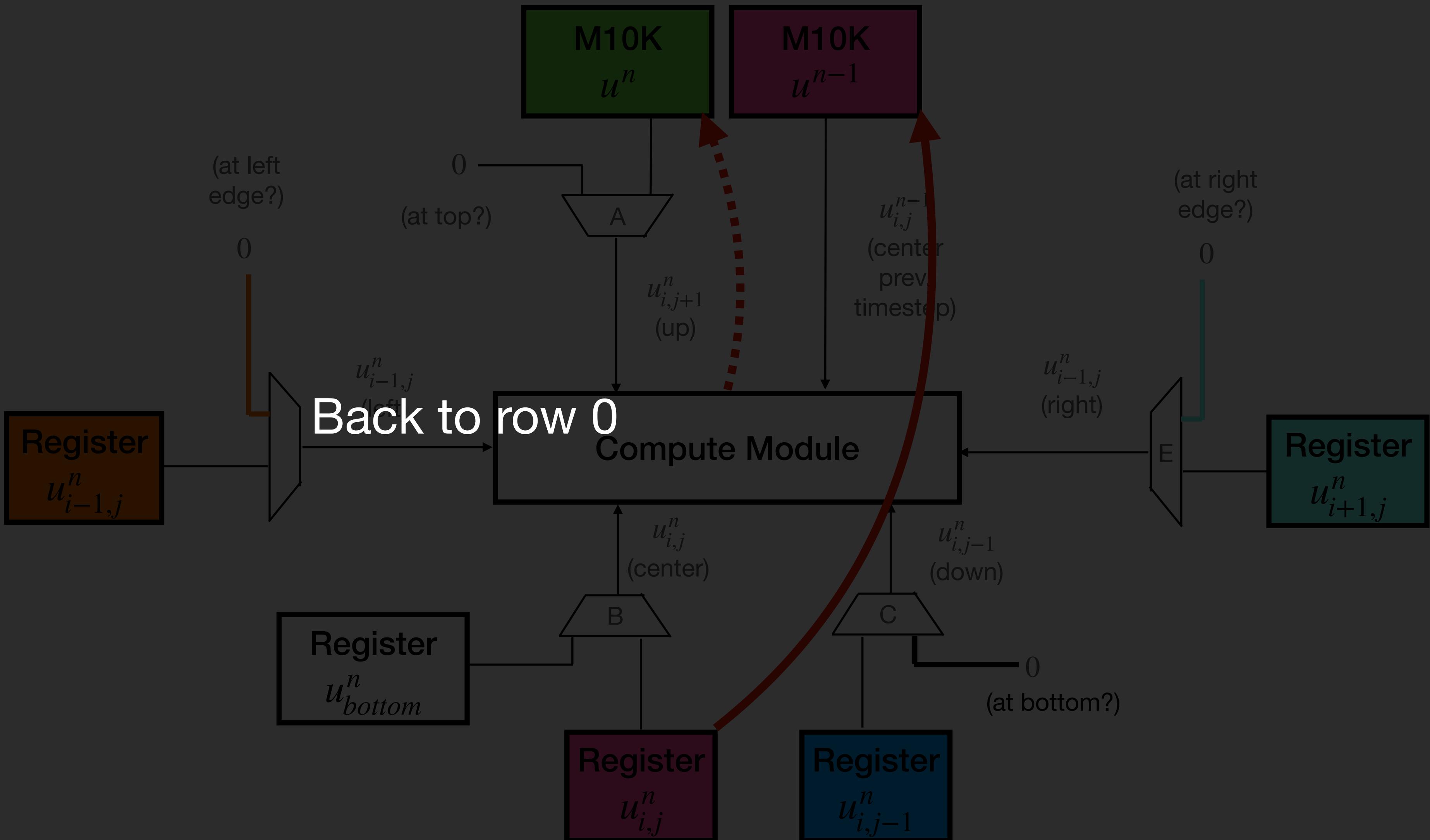
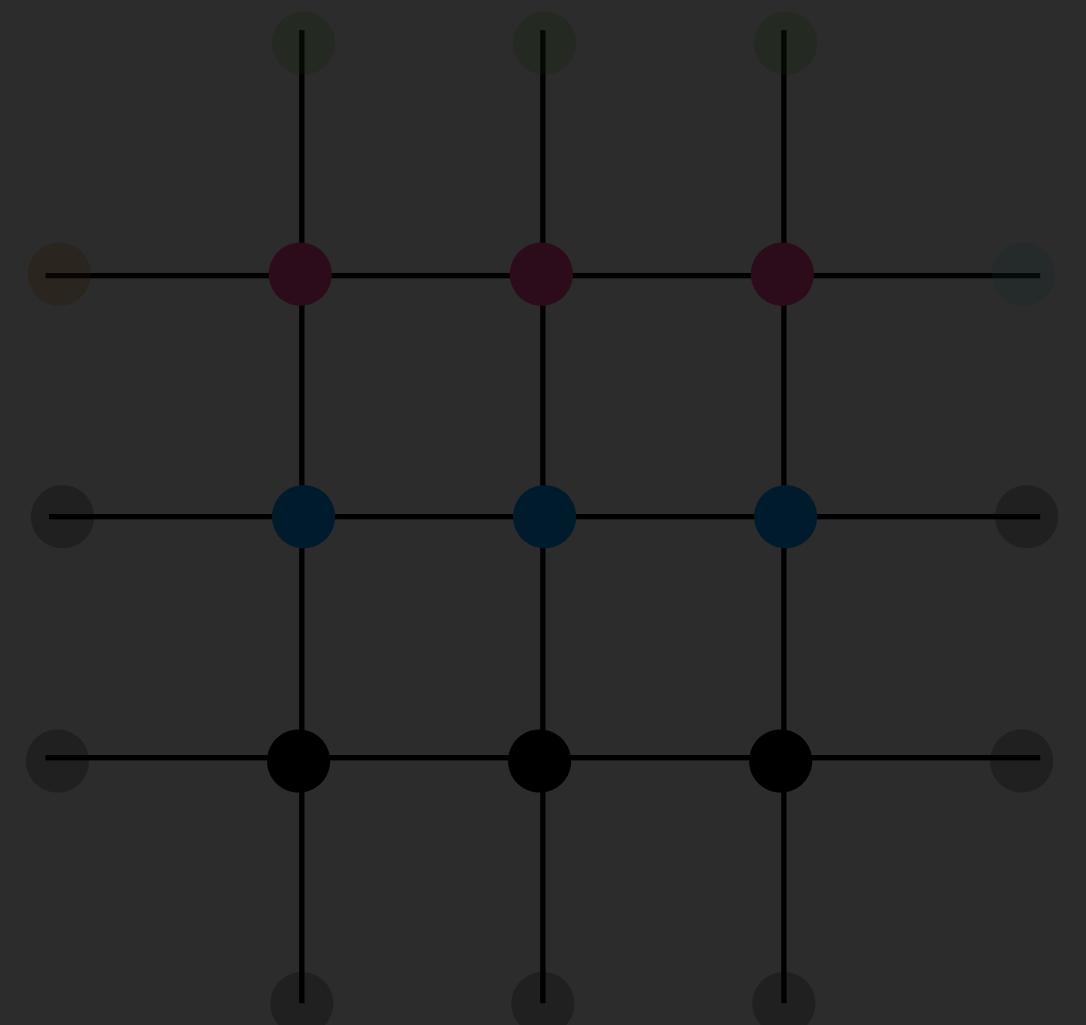
0 is multiplexed in for  
the “up node, the  
 $n - 1$  state of center  
node is read from  
M10K memory



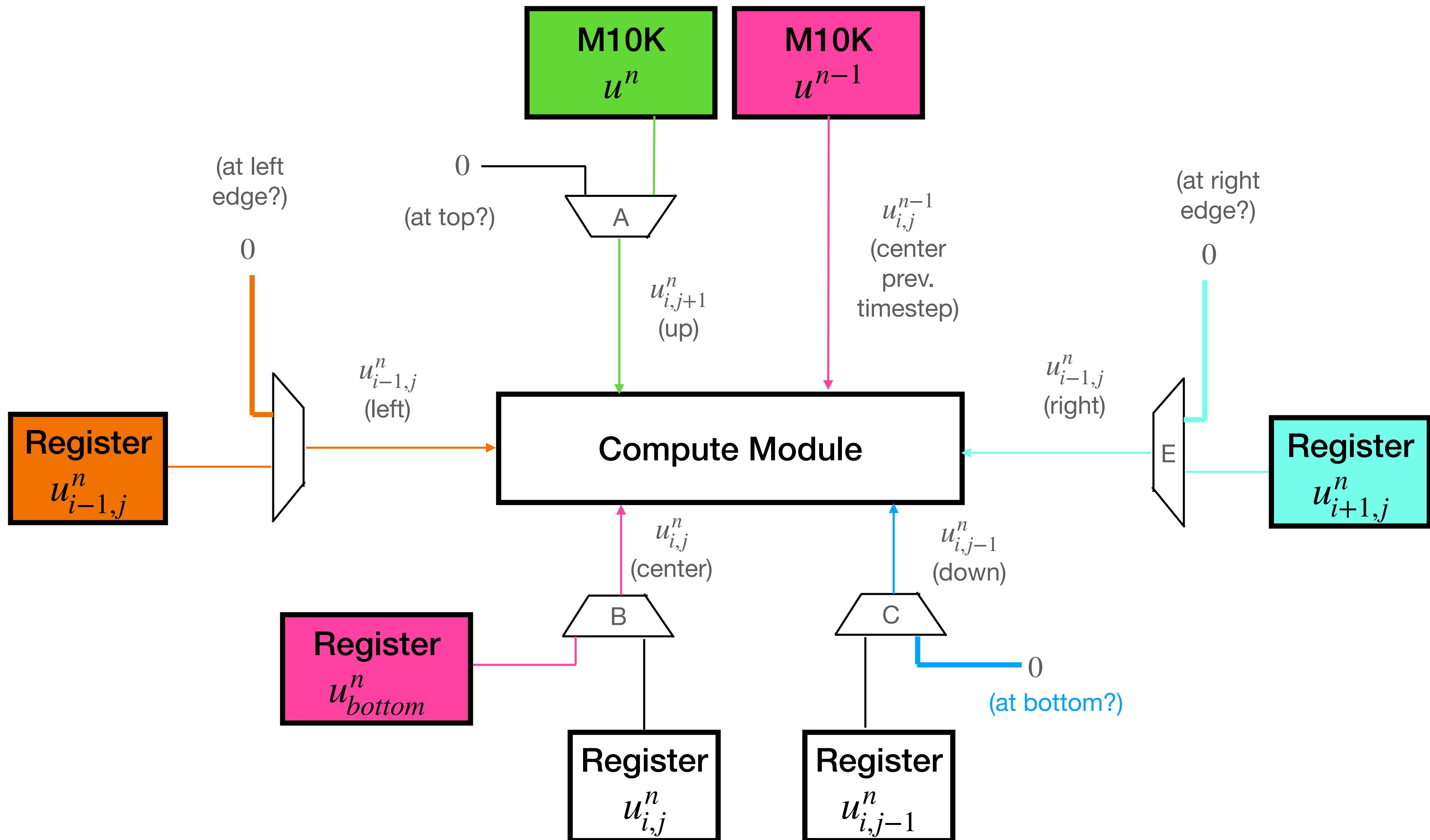
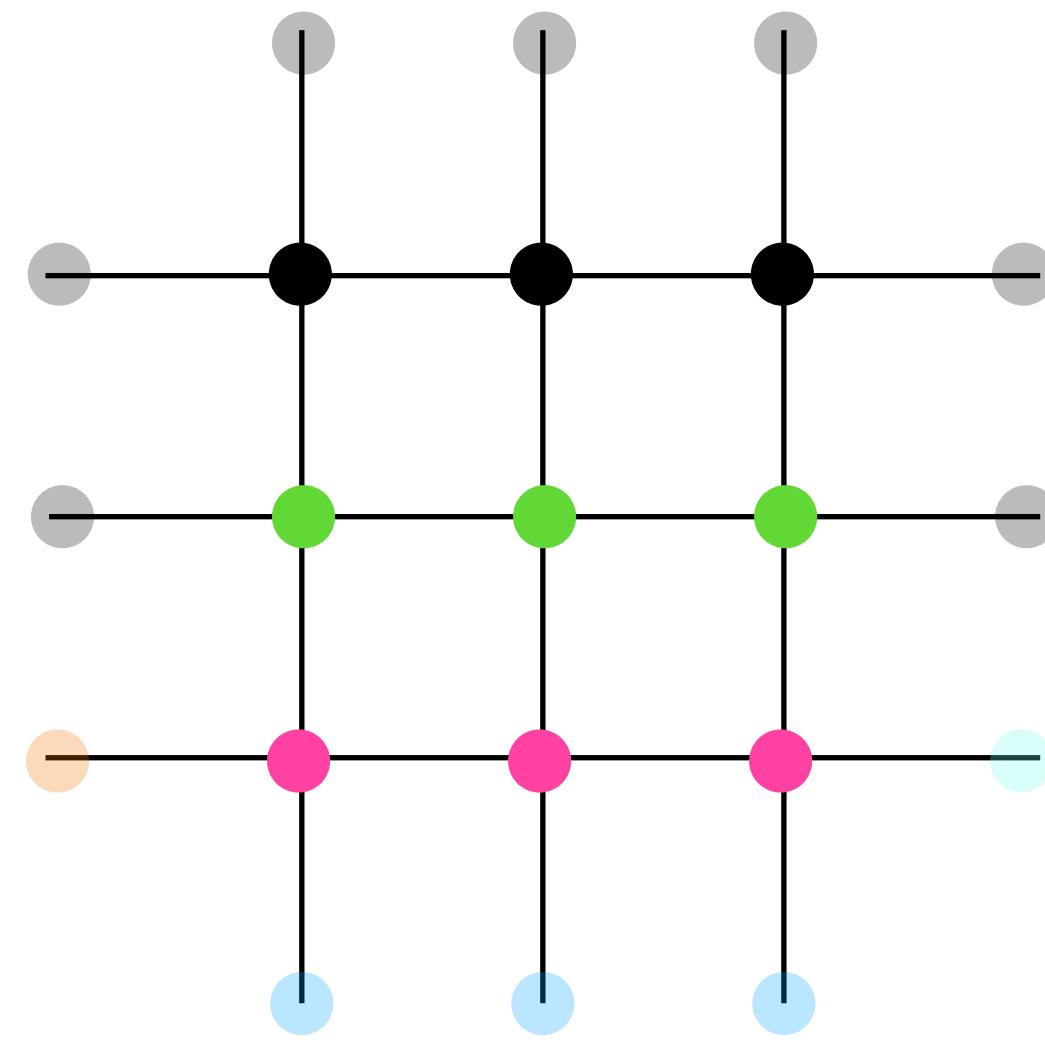
$u_{i,j}^{n+1} \rightarrow \text{M10k } n$  $u_{i,j}^n \rightarrow \text{M10k } n-1$ 

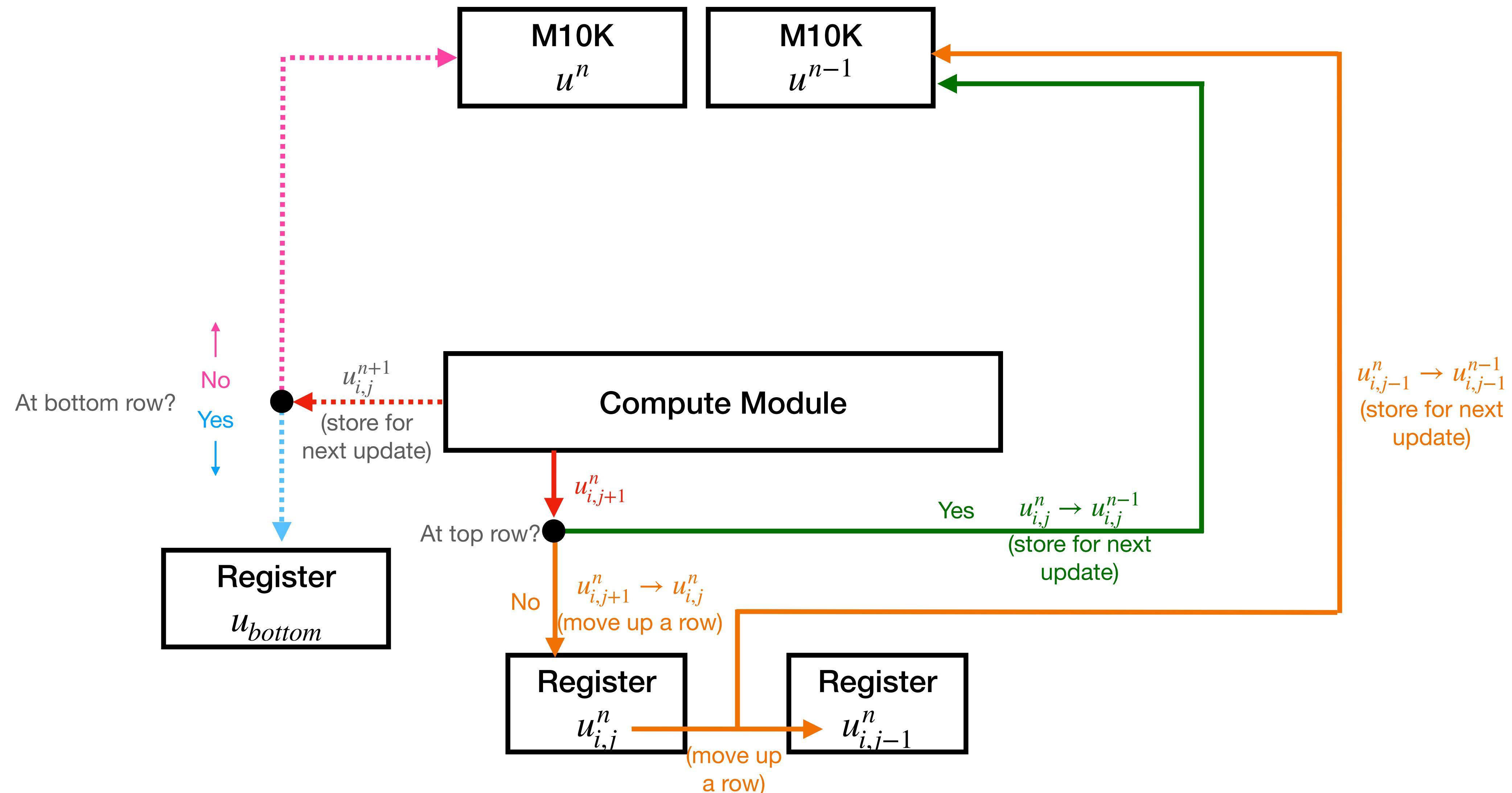
$u_{i,j}^{n+1} \rightarrow \text{M10k } n$

$u_{i,j}^n \rightarrow \text{M10k } n-1$



The “left” and “right” nodes are either the  $u_{bottom}^n$  registers from the adjacent columns, or 0





Solid line: pipelining information  
Dotted line: moving new information